

GOVERNMENT POLYTECHNIC

BHUBANESWAR-23



DEPARTMENT OF CIVIL ENGINEERING

LECTURE NOTES

Year & Semester: 3rd Year, 5th Semester

Subject code/Name -Th-2, STRUCTURAL DESIGN-II

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Steel Structure

* It is an assemble of a group of a members (columns) expected to sustain their share of applied forces and to transfer them safely to the ground.

Type of structure

on the basis of supporting system.

* Line structure (cable, beam, column)

* Surface structure

* Framed structure (space structure)

Structural Elements

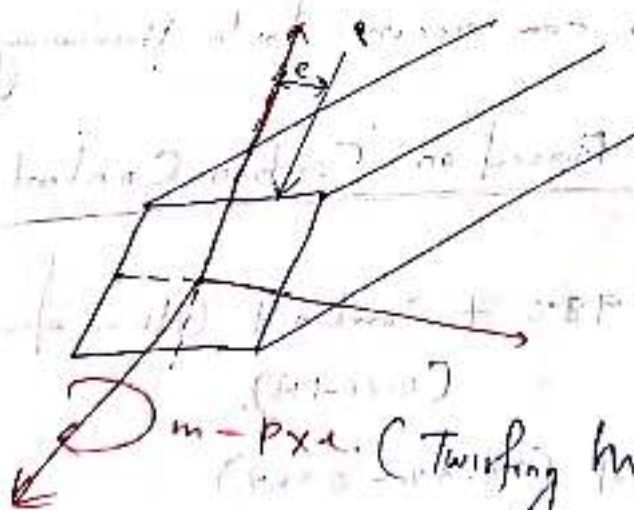
1) Tension Member

2) Compression Member

3) flexural Member

4) Beam - Column

5) Torsion - Member



Advantages of steel

- * Steel members have high strength per unit weight.
(Long span bridges, high-rise buildings).
- * Ductile materials. (% elongation $> 15\%$)
- * Conveniently handle and transported.
(% elongation $< 5\%$) brittle materials.
- * Modification can be easily done.
- * erected at faster rate.
- * Highest scrap value.
- * Properties of steel mostly do not change with time.
- * Properly maintained steel structures have a very long life.

Disadvantages

- * When placed in exposed condition, subjected to corrosion.
- * Steel structures need fire proof treatment.
- * Fatigue failure. (Reversal stress).
- * Thermal expansion can occur due to increasing Temp.

Classification of steel Based on Carbon Content.

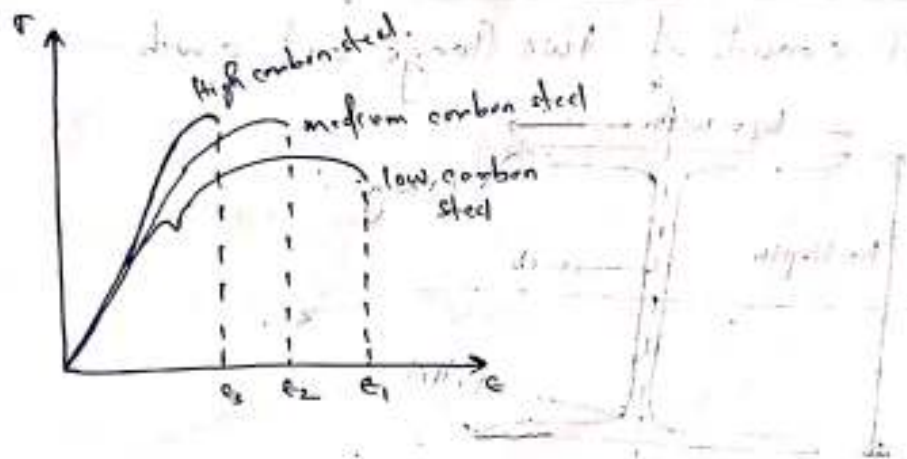
Iron (Fe) $> 98\%$ + Carbon + Other elements
($0.1\% - 1.1\%$).

- 1) Low carbon steel ($0.1\% - 0.25\%$)
- 2) Medium carbon steel ($0.25\% - 0.6\%$).
- 3) High carbon steel ($0.6\% - 1.1\%$)

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Various Iron-carbon Alloys.

- * Cast Iron - $> 2\%$ → Brittle, Hard, Rigid.
- * Steel - Carbon content (1% - 2%)
- * Wrought Iron Carbon Content $< 0.05\%$ (Soft weldable)



Rolled Steel Section

- * Steel is manufactured in rolling mill.
- * Hot steel is passed from series of rollers to get the desired shape.
- * Generally these shape are preferred which provide higher section modulus.

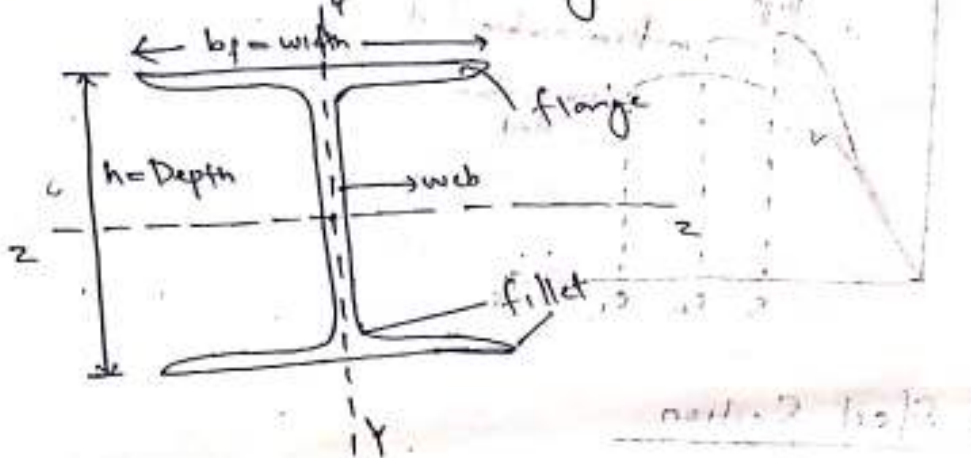
Types of Rolled steel Section

- 1) Rolled steel Beam Section (I)
- 2) Rolled steel Channel Section (C)
- 3) Rolled steel T-Section.
- 4) Rolled steel Angle Section. (It section manufactured in 1819)
- 5) Rolled steel Hollow Section.

- 6) Rolled steel plates.
- 7) Rolled steel flats.
- 8) Rolled steel Bars.
- 9) Rolled steel Strip
- 10) Rolled steel sheet.

1) Rolled steel Beam Sec (I-Section).

* It consists of two flange and a web.



Different Series of Beam Section

- * ISLB → Indian Standard Light Beam.
- * ISMB → Indian Standard Medium weight Beam. (Beam)
- * ISHB → Indian Standard Heavy weight Beam. (column)
- * ISWB → Indian Standard Wide flange Beam.
- * ISJB → Indian Standard junior Beam.

Beam Section are designated with depth of the section & Mass per unit length.

Eg:- ISWB 600 @ 50.6 kg/m.

depth

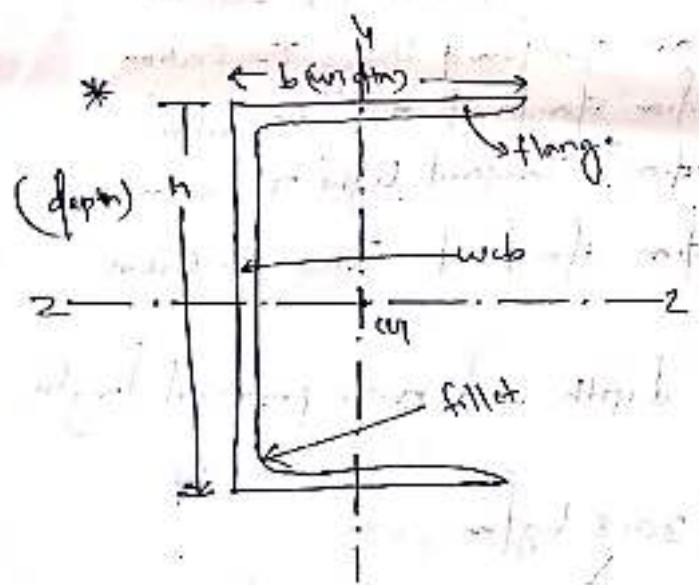
mass per unit length.

⇒ Rolled Steel Channel Section, (C).

- * Channel section are used as purlins in a roof truss.
- * Specially channel section are used to make built up Column Section.

following are the types of channel section.

- ① ISLC → Indian standard Light channel
- ② ISMC → Indian standard ^{medium} ~~Special~~ channel
- ③ ISSE → Indian standard Special channel
- ④ ISSJ → Indian standard Junior channel.



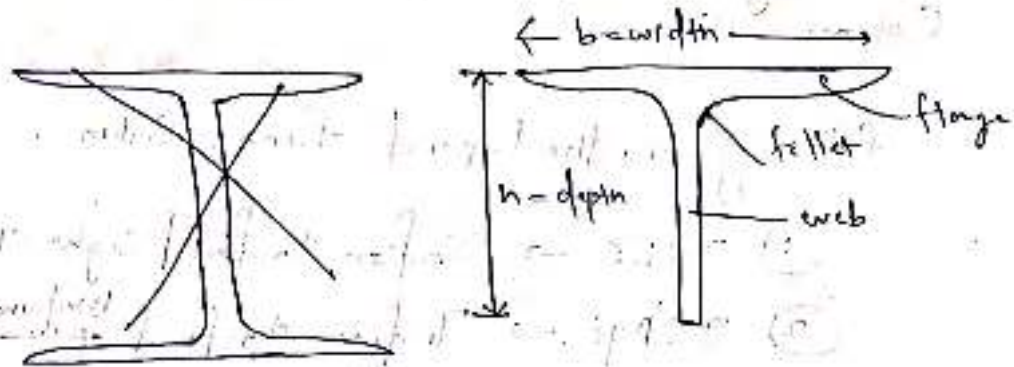
* they are designated with depth of section and mass per unit length.

ISMC 300 @ 30.8 kg/m
↓ ↓
depth (mm) mass per unit length.

3) Rolled Steel T-Section

* It has one flange and a web.

* T-sections are used in columns, bracket connection and in steel water tank.



There are 5 series of T-section.

- ① ISNT - Indian standard normal T-section
- ② ISHT - Indian standard Heavy T-section
- ③ ISST - Indian standard short T-section
- ④ ISLT - Indian standard light T-section
- ⑤ ISJT - Indian standard Junior T-section

* It is designated by depth and mass per unit length.

ISNT 200 @ 30.8 kg/m

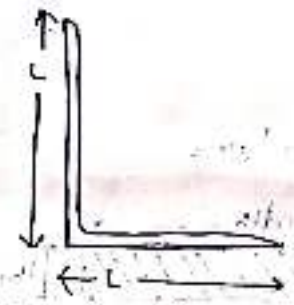
↓
d = 200 mm ↓
mass = 30.8 kg/m

4) Rolled Steel Angle Section

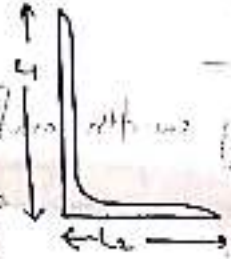
- * This is the 1st section to be manufactured.
- * Angle section are used to make builtup section, purlin's beam, stiffeners & to establish connection.

Angle section are 3 types

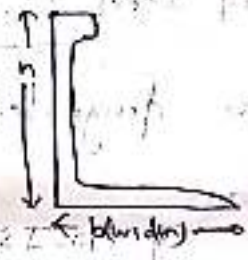
- ① Equal Angle Section
- ② Unequal Angle section
- ③ Bulb Angle section



(Equal angle sec)



(unequal angle sec)



(Bulb angle)

* Angle section are designed with both leg size & thickness

eg:- ISA 60x60x8 (equal angle)

ISA 100x60x8 (unequal angle)

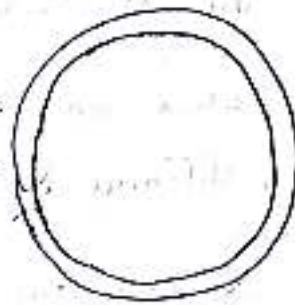
* Bulb angle section has consolidated area at one of the leg which provides stiffness to the angle.

* They are used in ship buildings & in gantry cranes.

5) Rolled steel tube Section

* They are designated by outside dimension, & thickness

* Hollow section are preferred in those member where torsion is dominant



There are 3 types of tube section.

- ① Square hollow section
- ② Rectangl. hollow section
- ③ Circular hollow section

6) Rolled steel flat.

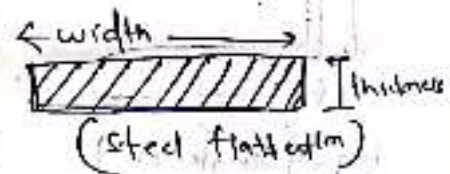
* They are designated by width and thickness.

For

eg: 100 ISF 10

100mm width of flat

10mm thickness of flat.



* flat sections are used in lacing system.

(Thickness of flat $t \geq 5$ mm)

(Generally length of flat upto ≤ 4000 mm)

7) Rolled steel Plate Section ($t \geq 5$ mm)

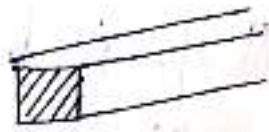
* It is designated by length, width and its thickness.

For eg:- ISPL 2000 x 1000 x 8

* Plate are used in column base.

* Gusset plate to form a connection between different members.

8) Rolled steel Bars



□ OI_d - 1 foot 0



○ OI_d - 1 foot 0

Steel bars are classified into 2 type

① Indian Standard Round bar (ISRD)

② Indian Standard Square Bar (ISQB)

* These section are designated by diameter in case of round bars and by sides in case of square bars.

Physical Property of steel

* Specific gravity of steel = 7.85

* Unit Mass of steel (ρ) = 7850 kg/m³

* Modulus of elasticity (E) = 2×10^5 mpa

* Poisson's Ratio (μ) = 0.30 (IS 800:2007)

* Modulus of Rigidity (G) = 0.769×10^5 mpa

* Coefficient of thermal expansion (α) = 12×10^{-6} /°C

Design Philosophy

① Loads

a) Dead load \rightarrow self weight of structural element

{ IS 875 (part-3) }

b) Imposed load \rightarrow Due to activities inside the structure

(Table furniture etc)

{ IS 875 (part-11) } (part-10)

c) Wind load \rightarrow It depends upon various factors

such as pressure intensity of the wind, topography, type of structure, shape & size and Risk coefficient.

{ IS 875 (part-11) }

d) Earthquake load & Seismic load - { IS 1893 }

Load Combination

	FOS (load factor):
\rightarrow DL + IL	\rightarrow 1.5
\rightarrow DL + WL/EL	\rightarrow 1.5
\rightarrow DL + IL + WL/EL	\rightarrow 1.2
\rightarrow DL + AL	\rightarrow 0.9 or 1.5

Type of Design Philosophies

① Working stress Method (WSM)

② Ultimate strength Method (USM)

③ Limit state Method (LSM)

① Working stress Method

Assumption

* Material behaves elastically

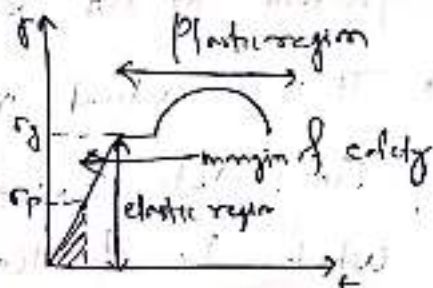
(C. Plastic strength of steel) - neglected

* Structural member designed for worstmost combination of loading.

* Uneconomical \rightarrow bcz. In this design we reduce stress by using a FOS.

$$\sigma_p = \sigma_y / FOS$$

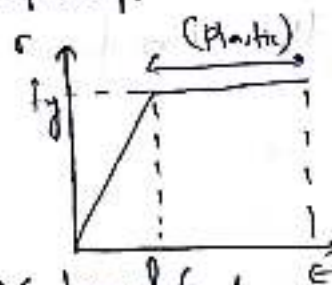
So, number of material required more.



② Ultimate strength Method (Plastic Method of design)

* In this method, Plastic region of stress strain curve of mild steel was also considered.

* Members are designed for collapse or ultimate load.



$$\text{Collapse load} = \text{working load} \times \text{load factor}$$

* The result of this method was section size requirement was smaller, hence economical. SP

* In this method 'serviceability' condition we are not considering. (Whether excessive deformation is occurs or not, Deflection, and vibration).

③ Limit state of Method

* In this method, the design objective is to make structure fit for use, for some target reliability.

* It is a statical method of design.

* Limit state considers all the possibilities because of which the structure will become 'unfit' for use.

There are two types of limit state

Limit state of strength

- * Strength (Yielding, buckling)
- * stability against overturning and sway.
- * for fracture due to fatigue
- * Plastic collapse.
- * Brittle fracture.

Limit state of serviceability

- * Deflection.
- * Vibration.
- * Fatigue check (Including repairable damage due to fatigue).
- * Corrosion.
- * fire.

size

Special Consideration in steel design:

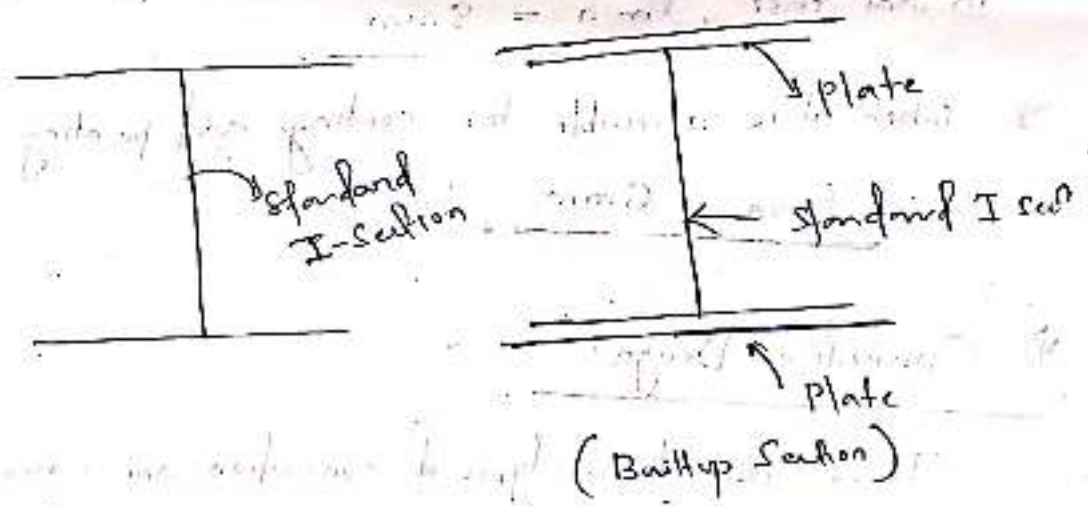
- 1) Size and Shape
- 2) buckling
- 3) Minimum thickness
- 4) Connection design.

① Size and shape

The members of steel structure should be designed to consist of any of the available sections, or combinations of them.

ex - A beam section may be a standard I-section or it may consist of builtup section.

②



② Buckling

The permissible load per unit area in steel is much higher as compared to permissible value in concrete.

Therefore the same load the cross-sectional area of a steel member is smaller.

* As the member in steel structure are more slender the compression member in steel structure are liable to buckling.

* To account for buckling the code specify that part of section be taken as ineffective.

Minimum Thickness

If very thin section are used a small amount of corrosion may result into large percentage reduction in effective area. hence minimum thickness to be used in structural member.

* When the member is directly exposed to weather & it is not accessible to perform coating or painting in that case, $t_{min} = 8\text{mm}$

* when it is accessible for coating and painting, $t_{min} = 6\text{mm}$.

4) Connection Design

There are three types of connection are commonly used.

- a) Riveted Connection
- b) bolted Connection
- c) welded Connection

①

nitgmb

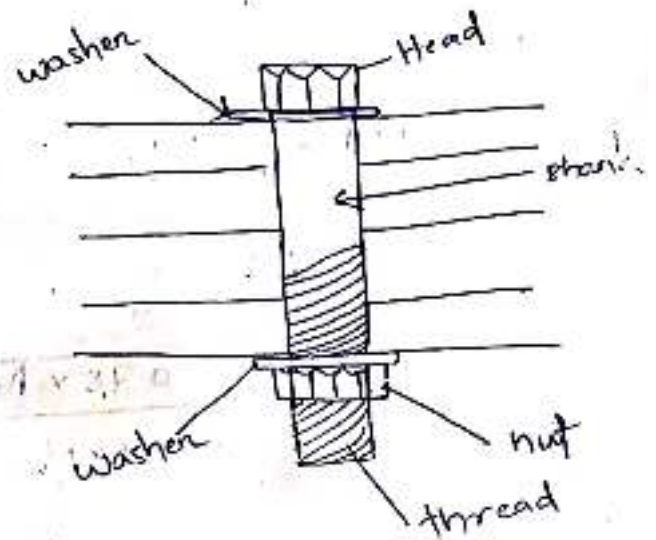
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Bolted connection

* Bolt can be defined as the piece of metal with head form at one end and shank threaded at other end.

* Threads are required to receive a nut.

*



Types of bolts

① Unfinished bolt

② High strength friction grip bolts (HSFG bolts)

① Unfinished bolts:

* They are also called as ordinary; Rough, Black & bearing type bolts.

* Unfinished bolts are made from low carbon steel circular steel.

* They are used when loading is static.

* They are not recommended when the loading is impact, vibration, Reversal of stresses.

* The size of ordinary bolt is in between 5 mm - 36 mm.

* Designated as M_{16} , M_{20} ,

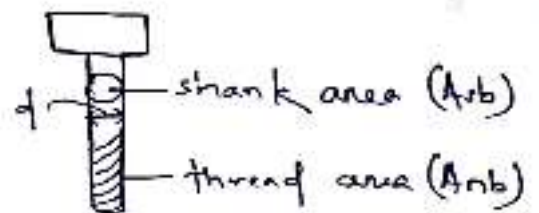
16 \rightarrow Diameter of bolts.

* The cross-sectional area at the threaded portion can be assumed equal to 0.78 times the shank area.

$$A_s = \frac{\pi}{4} \times d^2$$

$$A_{tb} = 0.78 \times A_s$$

$$= 0.78 \times \frac{\pi}{4} \times d^2$$



* Generally, the grade of bolt used is properly class 4.6.

4 \rightarrow 1st no \rightarrow Designate $\frac{1}{100}$ th of ultimate strength of bolt material.

$$f_{ub} = 4 \times 100 = 400 \text{ N/mm}^2$$

0.6 \rightarrow 2nd no \rightarrow Designated Ratio of yield strength and ultimate strength of bolts.

$$f_{yb} = 0.6 \times 400 = 240 \text{ N/mm}^2$$

* Bolt hole. (IS 800: 2007 - Pg No - 73 - (T-19) - (CL-10.2.1))

$$d < 12-14 \Rightarrow d_0 = 1 \text{ mm} + d$$

$$16 < d < 24 \text{ mm} \Rightarrow d_0 = 2 \text{ mm} + d$$

$$d > 24 \text{ mm} \Rightarrow d_0 = 3 \text{ mm} + d$$

- * In this bolt clamping action is negligible, therefore frictional resistance is zero.
- * Hence load is transfer by bearing mechanism.

② High strength friction grip Bolt (HSFG) bolts.

- * These bolts are made from medium carbon steel.
- * Their strength is increased by the Quenching process or by adding alloys.
- * These bolts can be tightened up to a large degree as compared to ordinary bolts.
- * Due to which large clamping action is developed, hence frictional resistance is generated between connecting elements.
- * Load is transferred mainly by friction - mechanism.
- * These bolts are used when the loading is, Dynamic, impact & vibration.
- * Generally dia of HSFG Bolts is 12mm - 36mm.
- * Generally property class 10.9 S is used.

S → strength, $f_{ub} = 10 \times 100 = 1000 \text{ N/mm}^2$
 $f_{yb} = 1000 \times 0.9 = 900 \text{ N/mm}^2$

- * Due to tightening of nut bolt is pre-tensioned which generates friction between connecting elements.

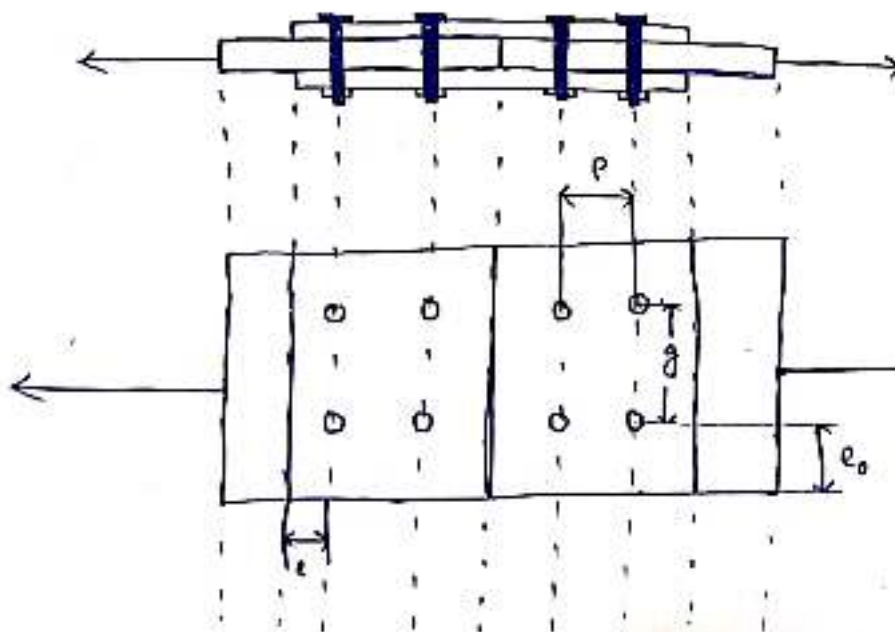
Advantages of Bolted connection.

- * Making joint is noise less.
- * Do not need skill labour.
- * Need less labour.
- * Connection can be made quickly.
- * Structure can be put to use immediately.
- * Modification if any can be done easily.
- * Working area required in the field is less.

Disadvantages of Bolted Connection

- * Due to vibration nuts are likely to loosen.
- * Rigidity of joints is reduced due to loose fit resulting into excessive deflection.

Different Terminology



- P = Pitch
- g = gauge
- e_0 = edge distance
- e = end distance

① Pitch (P)

It is the center to center distance between two consecutive bolt holes in the direction of parallel to apply force / stress.

* It is the center to center distance between two consecutive bolt holes measured in longer direction of connection.

* Minimum Pitch (P_{min}) - As per IS 800-2007 Page No. - 73
CL-10.2.2

$P_{min} = 2.5 \times d$ $\therefore d \rightarrow$ Nominal diameter of bolt.

* Maximum Pitch (P_{max}) = As per IS 800-2007 Page No. - 74
CL-10.2.3.2

① For Tension Member - (P_{max}) = $\frac{16t \text{ or } 200\text{mm}}{\text{min}^m}$

② For Compression Member (P_{max}) = $\frac{12t \text{ or } 200\text{mm}}{\text{min}^m}$
 $\therefore t \rightarrow$ Thickness of

* As per IS 800-2007 Page No. - 74, CL-10.2.3.1 -

The distance between the centers of any two adjacent bolts shall not exceed. $\frac{32t \text{ or } 300\text{mm}}$

$\therefore t \rightarrow$ Thickness of thinner plate.

② Gauge length (g).

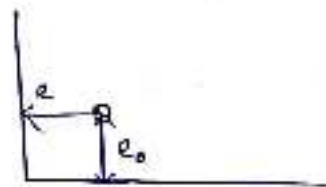
- * Center to center distance between two bolts measured in the direction perpendicular to applied force/stress.
- * In case of wide plate it is defined as the distance between two adjacent bolts measured in shorter direction.

End distance (e)

- * It is the distance between center of bolt to the nearest edge of the member in the direction of applied force.

Edge distance (e₀)

- * It is the distance between the center of bolts to the nearest edge of the member measured in the direction perpendicular to applied force/stress.



- * According to IS 800-2007 cl-10.2.4.2 Pg No-74
Minimum value of end & edge distance.

$$\begin{aligned} (e \& e_0) \text{ minimum} &= 1.7 \times d_0 \quad (\text{For hand flame cut}) \\ &= 1.5 \times d_0 \quad (\text{For machined flame cut}) \end{aligned}$$

$\therefore d_0 \rightarrow$ Diameter of bolt holes.

* According to IS 800:2007 cl-10.2.4.3 Page-74.

For Maximum value of e .

$$(e)_{\max} \rightarrow 12t e \quad \therefore t \rightarrow \text{thickness of thinner member}$$

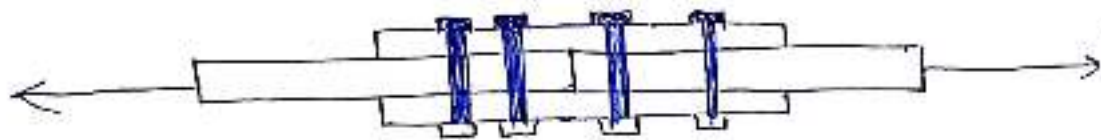
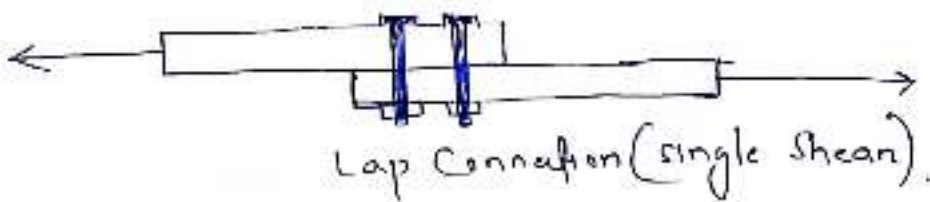
$$e = \sqrt{\frac{250}{f_y}}$$

Types of Bolted Connection.

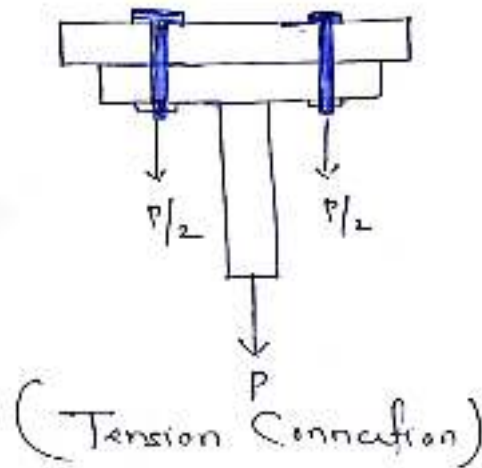
① On the basis of types of ~~bolt~~ force in the bolt.

a) Shear Connection: — Bolt are subjected to shear stress at a single or multiple cross-section.

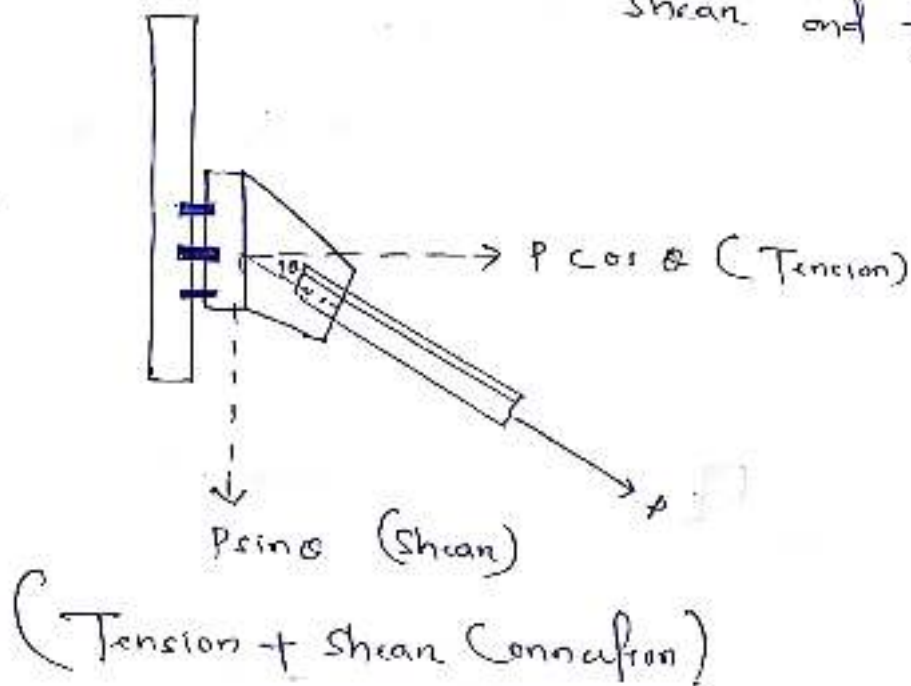
Exeg:- Lap Connection,
Butt Connection.



b) Hanger Connection → In this connection bolt cross-section will be under tensile stress.



→ Inclined bracket connection → Bolt are under combined state of stress due to shear and tension.

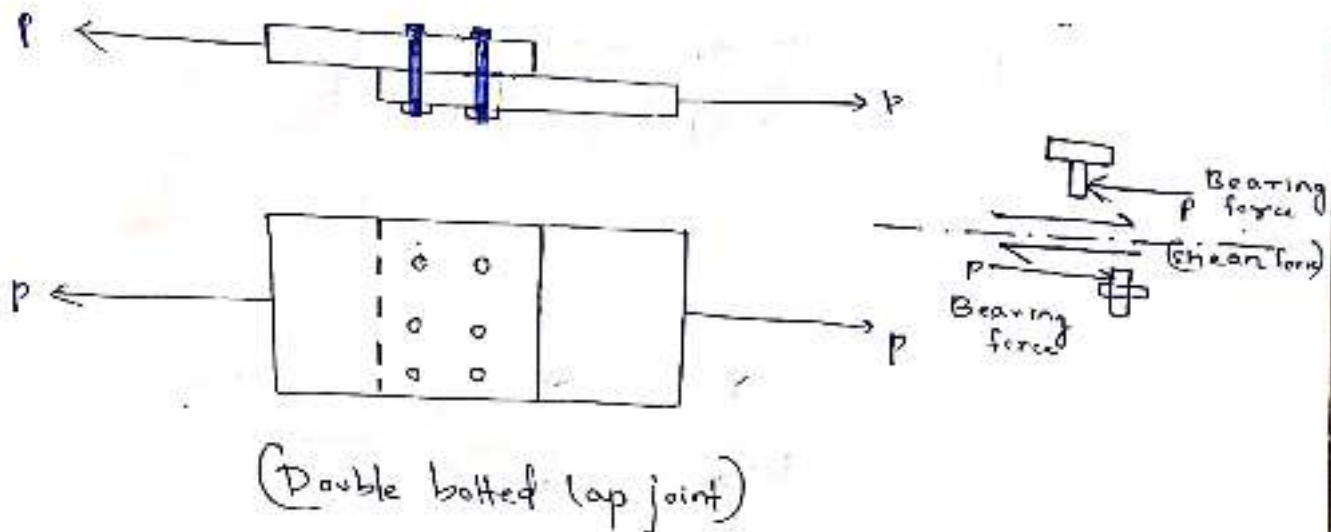


Types of bolted joint

- ① Lap joint
- ② Butt joint
 - Single cover butt joint
 - Double cover butt joint

① Lap joint

* When two structural elements are overlapped with each other then the joint formed is called Bolted Lap joint.



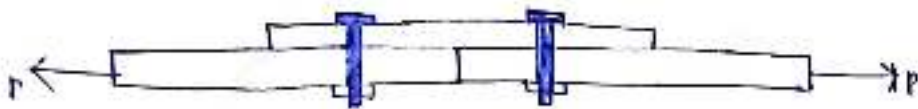
* The bolt will fail mainly due to shear.

② Butt joint

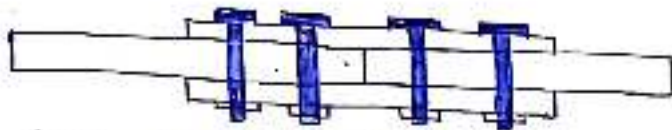
* In this joint the elements to be connected are placed edge to edge and then cover plate is provided at the top or all the top and bottom of the element.

* If the cover plate is provided only at top \rightarrow single cover butt joint

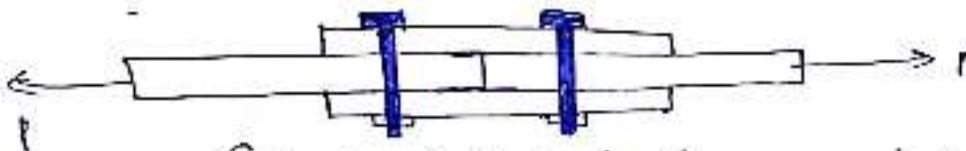
* If the cover plate is provided on both side \rightarrow Double cover butt joint.



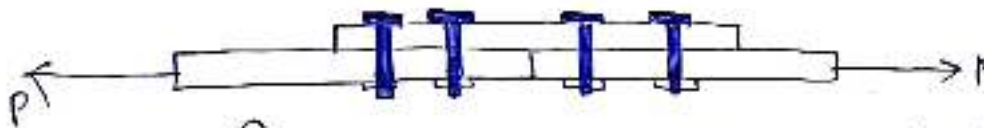
(Single bolted single cover butt joint)



(Double bolted double cover butt joint)



(Single bolted double cover butt joint)

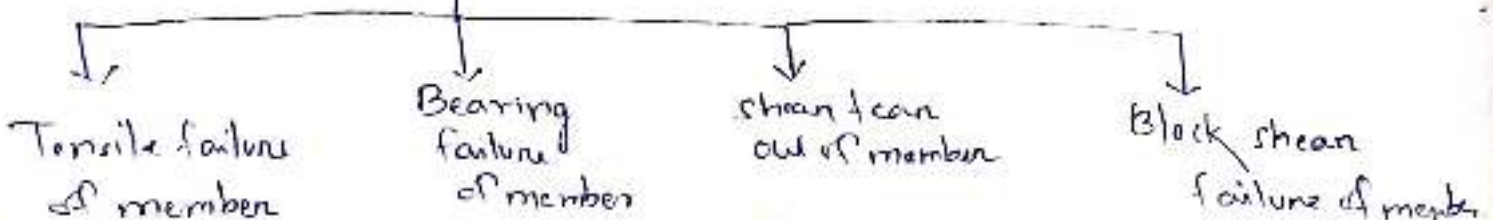


(Double bolted single cover butt joint)

Failure of bolted joint

failure of bolted joint can occur in two ways.

- ① failure of bolt
 - shear failure of bolt
 - Bearing failure of bolt
 - Tensile failure of bolt
- ② failure of Member.



Strength of bolted joint (Bearing-type bolts) (Unfinished bolts)

Assumption

- * Frictional resistance between the connected elements will be neglected.
- * All the bolts will share the load equally.
- * Any undesirable bending stress will be neglected.
- * The stress distribution is assumed to be uniform.

① Design shear strength of bolts.

- * The nominal shear strength of bolt depends upon grade of bolt, no. of shear planes & location of shear planes.

$$V_{nsb} = \frac{f_{ub}}{\sqrt{3}} [n_s \times A_{sb} + n_t \times A_{tb}]$$

(IS 800-2007)
Pg 40 - 75
cl-10.3.3

- ∴ V_{nsb} - Nominal shear capacity of a bolt
- f_{ub} - Ultimate tensile strength of bolt
- n_s → no. of shear plane intercepting in the shank portion.
- n_t → no. of shear plane intercepting in the threaded portion.
- A_{sb} → Shank Area
- A_{tb} → Threaded Area = $0.78 \times A_{sb}$.

Case-1 - Lap joint or single cover butt joint [1 shear plane]

$$n_s = 1, \quad n_n = 0$$

$$n_s = 0, \quad n_n = 1$$

Case-II Double cover butt joint [2 shear plane]

$$n_s = 2, \quad n_n = 0$$

$$n_s = 0, \quad n_n = 2$$

$$n_s = 1, \quad n_n = 1$$

Design shear capacity of Bolt

$$V_{dsb} = \frac{V_{nsb}}{\gamma_{mb}}$$

Partial Safety Factor
(IS 800-2007
Pg No-30, T-5, cl-5.4.3)

$$V_{dsb} = \frac{f_{ub}}{3 \times \gamma_{mb}} \times [n_s \times A_{sb} + n_n \times A_{nb}] \quad (\gamma_{mb} = 1.25)$$

* Reduction factor

① Reduction factor for long joint [IS 800-2007 Pg No-35
cl No-10.3.3.1]

* When the distance between first and last bolts in the joints measured in the direction of load transfer exceeds $15 \times d$. The nominal shear capacity V_{nsb} reduced by factor (β_{lj}) .

$$\beta_{lj} = 1.075 - \frac{L_j}{200d}$$

If $L_j > 15d$

$L_j \rightarrow$ length of joint.

② Reduction Factor for Large grip length [IS 800 2007 Pg No-75, cl-10.3.3.3]

* Grip length 'L_g' equal to total thickness of connected plates exceed 5x d, then shear capacity reduced by Reduction factor (β_{lg}).

$$\beta_{lg} = \frac{8d}{3d + L_g}$$

d = nominal dia of bolt.

③ Reduction Factor due to Packing Plate:- [IS 800 2007 Pg No-75, cl-10.3.3.3]

* If the thickness of packing plate 't_{pkg}' > 6mm then bending effect are generated in the bolt.

* Due to which shear capacity of the bolt is reduced by reduction factor 'β_{pkg}'

$$\beta_{pkg} = 1 - 0.0125 \times t_{pkg}$$

④ Bearing strength of Bolt. [IS 800-2007, Pg-75, cl-10.3.4]

* Bolt failure will occur, if high grade plates are connected using low grade of bolts.

* Bearing strength is independent of the grade of bolt.

* Bearing strength is dependent upon arrangement of bolt holes in the plate. (Gap between bolt holes, e, e₁)

* Nominal Bearing strength of bolt.

$$V_{npb} = 2.5 \times f_u \times d_t \times k_b$$

where,

f_u → Ultimate tensile stress of plate.

d → Nominal diameter of bolt.

t → Thickness of thinner main plate
or
Subtraction of cover bolt joint plate } \min^m

k_b :- Bearing factor
depends upon

$$\left. \begin{array}{l} \text{i) } \frac{e}{3d_0} \\ \text{ii) } \frac{p}{3d_0} - 0.25 \\ \text{iii) } \frac{f_{ub}}{f_u} \\ \text{iv) } 1 \end{array} \right\} \min^m \Rightarrow k_b$$

$\therefore d_0$ → diameter bolt hole

p → Pitch

e → end distance

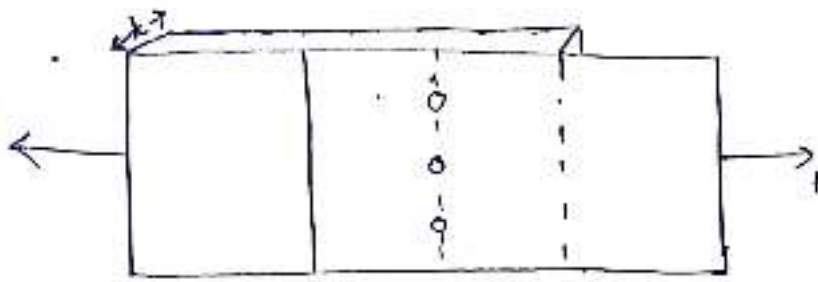
f_{ub} → Ultimate tensile stress of bolt.

Design Bearing strength of bolt $(V_{dpb}) = \frac{V_{npb}}{\gamma_{mb}}$

$\therefore \gamma_{mb} = 1.25$ (Pg-31, T-5).

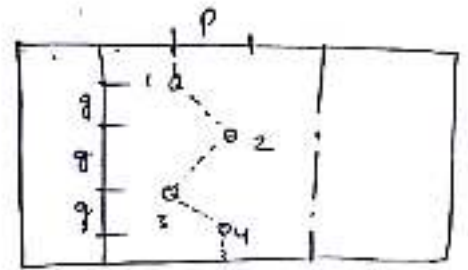
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③ Design Tensile strength of plate. (T_{dp}). [IS 800-2007
Pg No-32. C-6.3.1]



(Chain pattern)

$$A_n \rightarrow (B - 3 \times d_o) \times t$$



(Staggered pattern)

$$A_n = \left[B - 4 \times d_o + \frac{p^2}{4g} \times 3 \right] \times t$$

In general

$$A_n = (B - n \times d_o) \times t$$

* Staggered pattern of bolting is better than the chain pattern. Because it provides large value of net sectional area in tension (A_n).

$$\text{Staggered pattern } (A_n) = \left[B - n d_o + \sum_{i=1}^{n'} \frac{p_s^2}{4g_i} \right] \times t$$

$B \rightarrow$ width of plate

$n \rightarrow$ no. of bolt holes at the section consider

$d_o \rightarrow$ Diameter of bolt holes.

$n' \Rightarrow$ no. of staggered pitch travel by crack

$p_s \Rightarrow$ Staggered pitch.

$g \Rightarrow$ Gauge Distance.

$t \Rightarrow$ Thickness of thinner Main member.

Design Tensile strength of plate.

$$T_{dp} = \frac{0.9 \times f_u \times A_n}{\gamma_{m2}}$$

$\therefore \gamma_{m2} \rightarrow$ Partial safety factor for member resisting.

$\gamma_{m2} = 1.25$ [IS 800-2007, Pg-32, T-5]

$f_u \rightarrow$ ultimate tensile stress of plate.

$A_n \rightarrow$ Net sectional area.

4) Efficiency of Joints.

* Efficiency of bolted joint is defined as the percentage of load that can be transferred by a bolted joint in terms of the strength of solid plate.

$$\text{Efficiency of joint } (\eta) = \frac{\text{Strength of joint}}{\text{Strength of Solid plate}} \times 100$$

Strength of joint := $\min^m \left\{ \begin{array}{l} 1) \text{ shear strength of bolt} \\ 2) \text{ Bearing strength of bolt} \\ 3) \text{ Tensile strength of plate} \end{array} \right\}$ (Bolt value)

$$\text{Strength of Solid plate} = (T_{dg}) = \frac{A_g \times f_y}{\gamma_{m0}} \quad \left[\begin{array}{l} \text{Pg No-32} \\ \text{C-5.2} \end{array} \right]$$

$A_g \rightarrow$ gross area of cross section.

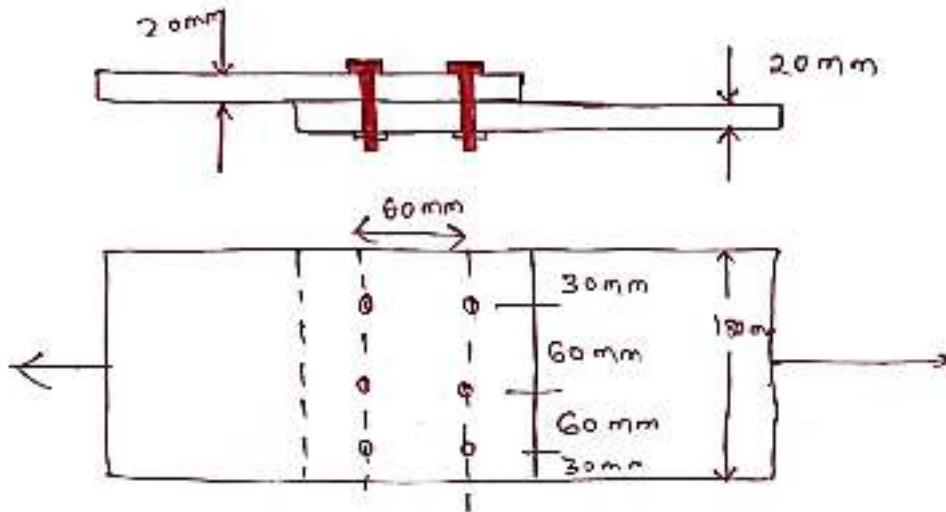
$f_y \rightarrow$ yield stress of materials.

$\gamma_{m0} \rightarrow$ Partial safety factor = 1.1 (Pg-30, T-5).

9

Question - 1

find the efficiency of a lap joint are shown in fig. M_{20} bolts of grade 4.6 and Fe410 (E250) plate are used.



Data given

for 4.6 grade of bolt

$$f_{ub} = 4 \times 100 = 400 \text{ N/mm}^2$$

$$f_{yb} = 400 \times 0.6 = 240 \text{ N/mm}^2$$

$$f_u = 410 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

thickness of plate = 20mm

width of plate (B) = 180mm

diameter of bolt (d) = 20mm

Diameter of bolt holes (d_0) = $20 + 2 = 22 \text{ mm}$

① Tensile strength of plate

$$\begin{aligned} \text{Net sectional area } (A_n) &= (B - nd) \times t \\ &= (180 - 3 \times 22) \times 20 \\ &= 2280 \text{ mm}^2. \end{aligned}$$

$$\begin{aligned} T_{dp} &= \frac{0.9 \times f_u \times A_n}{\gamma_{mc}} \\ &= \frac{0.9 \times 410 \times 2280}{1.25} \\ &= 673056 \text{ N} \approx 673.056 \text{ kN}. \end{aligned}$$

② Strength of Bolt (Number of Bolt $\rightarrow 6$)

Shear strength of bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \times (n_s \times A_{sb} + n_n \times A_{nb})$$

Single shear, $n_s = 1$, $n_n = 0$ (Assume).

A_{sb} = Nominal shank area of bolt

$$A_{sb} = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 20^2 = 314.159 \text{ mm}^2$$

(Threaded Area of bolt) $A_{nb} = 0.78 \times A_{sb}$

$$= 0.78 \times 314.159 = 245.044 \text{ mm}^2.$$

10

Design shear strength of one bolt

$$\begin{aligned}
 V_{dsb} &= \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \times [n_s \times A_{sb} + n_o \times A_{ob}] \\
 &= \frac{400}{\sqrt{3} \times 1.25} \times [0 \times A_{sb} + 1 \times 245.044] \\
 &= 45272.39 \text{ N} \approx 45.272 \text{ kN}
 \end{aligned}$$

Design shear strength of 6 bolts

$$V_{dsb} = 45.272 \times 6 = 271.632 \text{ kN}$$

Bearing strength of bolt.

$$V_{dpb} = \frac{2.5 \times k_b \times d \times f_u}{\gamma_{mb}}$$

k_b :- Bearing factor

$$\Rightarrow \frac{e}{3d_1} = \frac{630}{3 \times 22} = 0.45$$

$$\Rightarrow \frac{p}{3d_0} - 0.25 = \frac{60}{3 \times 22} - 0.25 = 0.65$$

$$\Rightarrow \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$\Rightarrow 1$$

which one is Minimum

$$\therefore k_b = 0.45$$

Design
∴ Bearing strength of one bolt

$$V_{dpb} = \frac{2.5 \times 0.45 \times 20 \times 20 \times 410}{1.25}$$
$$= 147.60 \text{ kN}$$

∴ Bearing strength of 6 no of bolts.

$$V_{dpb} = 6 \times 147.60 = 885.6 \text{ kN.}$$

$$\text{efficiency of joint } (\eta) = \frac{\text{strength of joint}}{\text{strength of solid plate}} \times 100$$

$$\therefore \text{ strength of joint } \Rightarrow \min^m (271.63 \text{ kN}, 673.045 \text{ kN}, 885.6 \text{ kN})$$
$$\therefore \text{ strength of joint} = 271.63 \text{ kN}$$

$$\text{Strength of solid plate} = \frac{A_g \times f_y}{\gamma_{mo}}$$
$$= \frac{6 \times 20 \times 180 \times 250}{1.1}$$
$$= 818.81 \text{ kN}$$

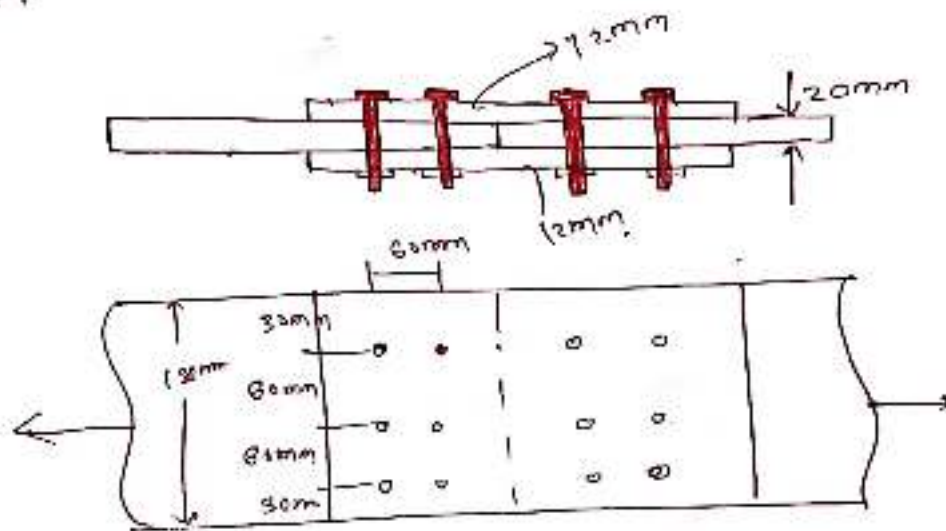
$$\text{efficiency of joint } (\eta) = \frac{271.63}{818.81} \times 100$$
$$= 33.17 \%$$

Dus

11

Question-2

find the efficiency of joint if in the above example instead of lap joint, but joint is made using two cover plate each of size 12 mm and 6 nos. of bolt on each plate.



Data given

$$f_{ub} = 400 \text{ N/mm}^2$$

$$f_u = 410 \text{ N/mm}^2$$

$$f_{yb} = 240 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

width of plate (B) = 180 mm

thickness of plate (t) = 20 mm

diameter of bolt (d) = 20 mm

diameter of bolt hole (d_0) = $20 + 2 = 22 \text{ mm}$

① Design Tensile of plate

$$\begin{aligned}\text{Net sectional area } (A_n) &= (B - nd) \times t \\ &= (180 - 3 \times 22) \times 20 \\ &= 2280 \text{ mm}^2\end{aligned}$$

Design Tensile strength of plate

$$\begin{aligned}T_{dpb} &= \frac{0.9 \times f_u \times A_n}{\gamma_{mc}} \\ &= \frac{0.9 \times 410 \times 2280}{1.25} \\ &= 673.056 \text{ kN.}\end{aligned}$$

Strength of Bolt

a) Design shear capacity of bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \times [n_s \times A_{sb} + n_t \times A_{tb}]$$

for double shear plane

$$\left. \begin{array}{l} n_s = 1 \\ n_t = 2 \end{array} \right\} \text{Assume.}$$

Shank Area

$$A_{sb} = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 20^2 = 314.159 \text{ mm}^2$$

Thread Area

$$A_{tb} = 0.78 \times A_{sb} = 245.044 \text{ mm}^2$$

(12)

Design shear capacity of one bolt

$$V_{dsb} = \frac{400}{3 \times 1.25} \times [1 \times 314.159 + 1 \times 245.04]$$

$$= 103.21 \text{ kN.}$$

Design shear strength of 6 bolts.

$$V_{dsb} = 6 \times 103.21 = 619.86 \text{ kN.}$$

b) Design Bearing stress of bolt.

$$V_{dps} = \frac{2.5 \times k_b \times d \times t \times f_u}{\gamma_{mb}}$$

k_b = Bearing factor.

$$k_b \Rightarrow \frac{e}{3d_0} = \frac{30}{3 \times 22} = 0.45$$

$$\Rightarrow \frac{P}{3d_0} - 0.25 = \frac{60}{3 \times 22} - 0.25 = 0.65$$

$$\Rightarrow \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$\Rightarrow 1$$

which
one is
Min?

$$\therefore k_b = 0.45$$

Design bearing stress of one bolt

$$V_{dps} = \frac{2.5 \times 0.45 \times 20 \times 20 \times 410}{1.25} = 147.60 \text{ kN.}$$

Design Bearing stress of 6 Nos of bolt.

$$V_{dpb} = 6 \times 147.60 = 885.6 \text{ kN.}$$

$$\text{Efficiency of joint } (\eta) = \frac{\text{Strength of joint}}{\text{Strength of solid plate}} \times 100$$

$$\therefore \text{Strength of joint} \rightarrow \min^m (673.056 \text{ kN}, 619.86 \text{ kN} \text{ \& } 885.6 \text{ kN})$$

$$\therefore \text{Strength of joint} = 619.86 \text{ kN.}$$

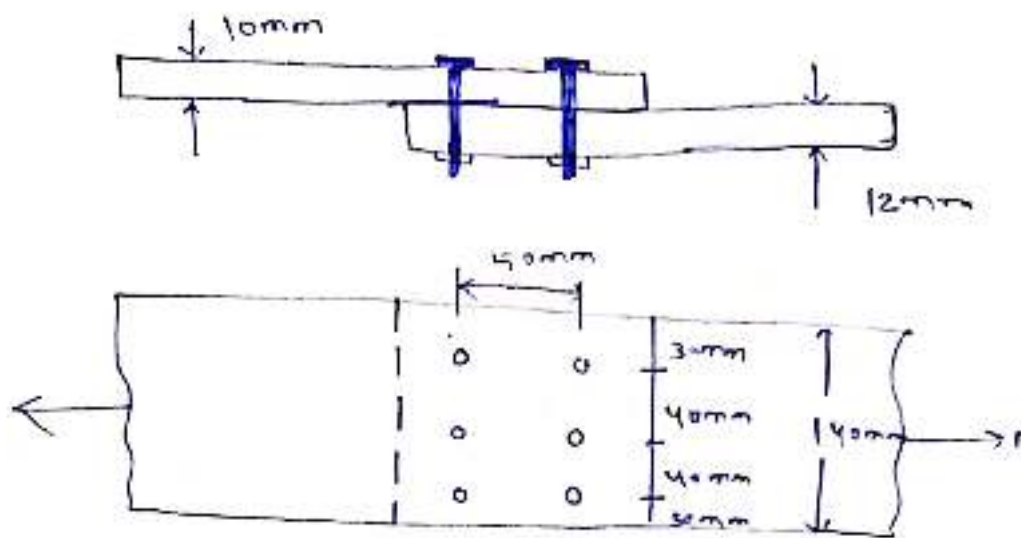
$$\begin{aligned} \therefore \text{Strength of Solid plate} &= \frac{A_g \times f_y}{\gamma_{mo}} \\ &= \frac{180 \times 20 \times 250}{1.1} \\ &= 818.18 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Efficiency of joint } (\eta) &= \frac{619.86}{818.18} \times 100 \\ &= 75.76 \%. \end{aligned}$$

\therefore Double cover joint having more efficiency than lap joint. So, DCBJ generally preferred.

Question-3

Find the maximum force that can be transmitted through a double bolted chain lap joint consisting of 6 bolts into two rows connecting two plates of thickness 12mm and 10mm given that M16 bolts of grade 4.6 and Fe250 plate used.



Data given

$$f_{ub} = 400 \text{ N/mm}^2$$

$$f_u = 410 \text{ N/mm}^2$$

$$f_{yb} = 400 \times 0.6 = 240 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

Diameter of bolt (d) = ~~16~~ 16 mm

Diameter of bolt hole (d_o) = $16 + 2 = 18$ mm

width of ~~thickness~~ plate (B) = 140 mm

thickness of plate (t) = 10 mm.

① Design tensile strength of plate

$$\begin{aligned}\text{Net sectional area } (A_n) &= (B - n d_0) \times t \\ &= (140 - 3 \times 18) \times 10 \\ &= 860 \text{ mm}^2\end{aligned}$$

Design tensile strength of plate

$$\begin{aligned}T_{dp} &= \frac{0.9 \times f_u \times A_n}{\gamma_{mL}} \\ &= \frac{0.9 \times 410 \times 860}{1.25} \\ &= 253.87 \text{ kN.}\end{aligned}$$

② Bolt strength.

a) Design shear capacity of Bolt.

$$V_{d,b} = \frac{f_{ub}}{\sqrt{3} \times \gamma_{mL}} \times [n_s \times A_{s,b} + m \times A_{t,b}]$$

Single shear

$$n_s = 1$$

$$m = 0$$

$$\text{Shank area } A_{s,b} = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 16^2 = 201.06 \text{ mm}^2$$

$$\text{Thread Area } (A_{t,b}) = 0.78 \times A_{s,b} = 0.78 \times 201.06 = 156.82 \text{ mm}^2$$

(14)

Design shear capacity of one bolt

$$V_{d1b} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \times [n_s \times A_{sb} + n_n \times A_{nb}]$$

$$= \frac{400}{\sqrt{3} \times 1.25} \times [0 \times A_{sb} + 1 \times 156.82]$$

$$= 28.97 \text{ kN}$$

∴ Design shear capacity of 6 Nos of Bolts.

$$V_{b1b} = 28.97 \times 6 = 173.82 \text{ kN.}$$

b) Design Bearing stress of Bolt

$$V_{d1b} = \frac{2.5 \times k_b \times d \times t \times f_u}{\gamma_{mb}}$$

k_b = Bearing factor

$$\Rightarrow \frac{e}{3d_0} = \frac{30}{3 \times 18} = 0.55$$

$$\Rightarrow \frac{p}{3d_0} - 0.25 = \frac{50}{3 \times 18} - 0.25 = 0.63$$

$$\Rightarrow \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$\Rightarrow 1$$

whichever
is minⁿ

$$\therefore k_b = 0.55$$

Design Bearing capacity of one bolt

$$V_{d1b} = \frac{2.5 \times 0.55 \times 16 \times 10 \times 410}{1.25} = 72.16 \text{ kN}$$

Design Bearing capacity of 6 Nos of Bolt = 6×72.16
= 432.96 kN

$$\therefore \text{Strength of joint} = \min(253.87 \text{ kN}, 173.82 \text{ kN}, 432.98 \text{ kN})$$

$$\therefore \text{Strength of joint} = 173.82 \text{ kN}$$

\therefore Maximum force can be transmitted in joint is 173.82 kN.

Design of Bolted joint

Question

Design a lap joint between the two plates each of width 120 mm, if the thickness of plates are 16 mm and 12 mm. The joint has to transfer a design load of 160 kN. The plate are of Fe 410, use bearing type bolt.

Data Given

Assuming 4.6 property class and M16 grade of bearing type bolt

$$f_{ub} = 400 \text{ N/mm}^2$$

$$f_{yb} = 400 \times 0.6 = 240 \text{ N/mm}^2$$

$$f_u = 410 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

$$\text{width of plate (B)} = 120 \text{ mm}$$

$$\text{Diameter of bolt (d)} = 16 \text{ mm}, d_o = 16 + 2 = 18 \text{ mm}$$

$$\text{thickness of plate} = 12 \text{ mm}$$

$$e = 1.5 \times d_o \text{ (flange edge)}$$

$$= 1.5 \times 18 = 27 \approx 30 \text{ mm}$$

$$p = 2.5 \times d = 2.5 \times 16 = 40 \text{ mm}$$

① Bolt strength

a) Design shear capacity of Bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \times \gamma_{mb}} \times [n_s \times A_{sb} + n_n \times A_{nb}]$$

Cap joint \rightarrow Single Shear

$$n_n = 1$$
$$n_s = 0$$

$$\text{Shank Area } (A_{sb}) = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 16^2 = 201.06 \text{ mm}^2$$

$$\text{Threaded Area } (A_{nb}) = 0.7854 \times A_{sb} = 0.7854 \times 201.06 = 156.82 \text{ mm}^2$$

Design shear capacity of a bolt

$$V_{dsb} = \frac{400}{\sqrt{3} \times 1.25} \times [1 \times 156.82]$$
$$= 28.97 \text{ kN.}$$

b) Design Bearing stress of a bolt

$$V_{dpsb} = \frac{2.5 \times k_b \times d \times t \times f_u}{\gamma_{mb}}$$

$k_b \Rightarrow$ Bearing factor

$$\Rightarrow \frac{e}{3d_0} = \frac{30}{3 \times 18} = 0.55$$

$$\Rightarrow \frac{f}{3d_0} - 0.25 = \frac{40}{3 \times 18} - 0.25 = 0.49$$

$$\Rightarrow \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

} which are
100%
-

$$\therefore k_b = 0.49$$

Design Bearing stress of bolt.

$$V_{dpb} = \frac{2.5 \times 16 \times 12 \times 0.49 \times 410}{1.25}$$

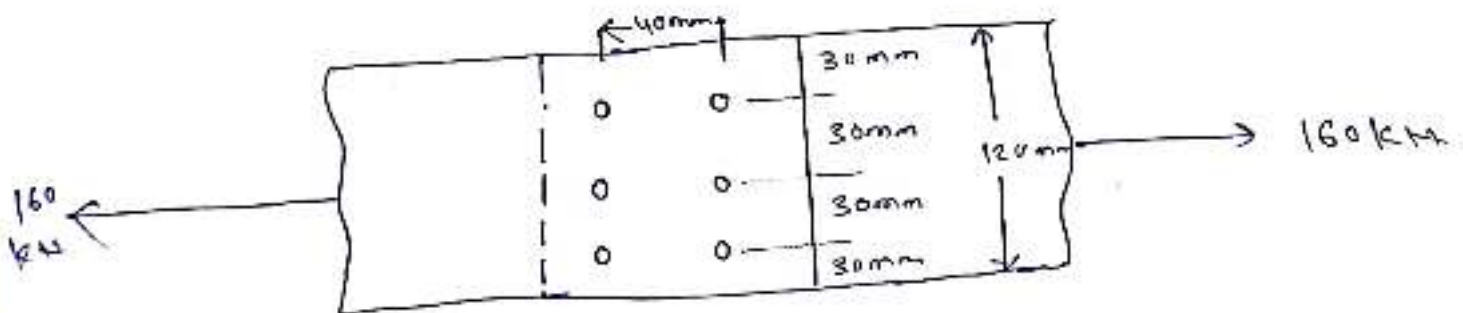
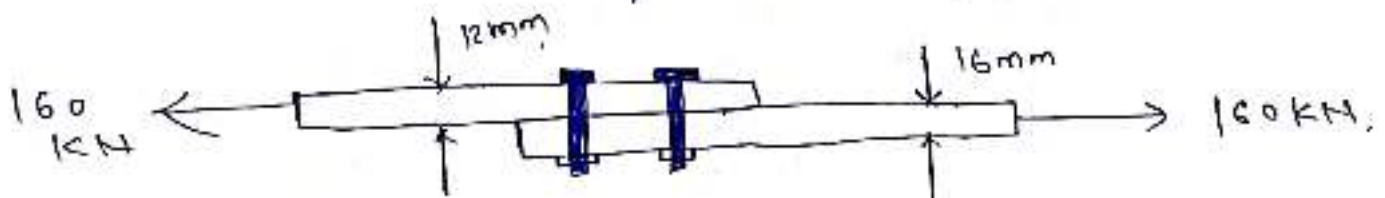
$$= 77.145 \text{ kN.}$$

$$\therefore \text{Bolt value} = \min(28.97 \text{ kN}, 77.145 \text{ kN})$$

$$\therefore \text{Bolt value} = 28.97 \text{ kN.}$$

Total factored load = 160 kN.

$$\text{No of Bolts required} = \frac{160}{28.97} = 5.5228 \text{ nos.}$$



Check

Design Tensile strength of plate.

$$T_{dp} = \frac{0.9 \times f_u \times A_n}{\gamma_{m1}}$$

(16)

Net sectional Area of plate

$$\begin{aligned} A_n &= (B - nd_0) \times t \\ &= (120 - 3 \times 18) \times 12 \\ &= 792 \text{ mm}^2. \end{aligned}$$

Design Tensile strength of plate

$$\begin{aligned} T_{dp} &= \frac{0.9 \times 410 \times 792}{1.25} \\ &= 233.79 \text{ kN} > 160 \text{ kN} \\ &\quad (\text{Design is safe}) \end{aligned}$$

~~Q1~~ Question - 2

Design a lap joint to connect two plates 300mm wide and 16mm thick using 20mm diameter of bolts of property class 4.6, then the applied factored load 370 kN.

Anshuman

Shearing Capacity of HSFU Bolt. (IS 800-2007, Pg-76, Cl-10.4)

* These are the bolts made of high tensile steel which are pretensioned and their resistance to shear force is mainly by friction.

* Nominal shear capacity of HSFU Bolt. (IS 800-2007, Pg-76, Cl-10.4.3)

$$V_{nsd} \Rightarrow \mu_f \times n_s \times k_n \times F_o$$

Where,

F_o = Pretension force, KN

$$F_o = f_o \times A_{nb}$$

A_{nb} = net Area of bolt

f_o = proof stress = $0.7 \times f_{ub}$

f_{ub} = Ultimate strength of bolt

n_s = no. of shear interface offering frictional resistance.

k_n = Hole factor

$\Rightarrow 1$ (Standard sized holes)

$\Rightarrow 0.8$ (Over sized holes

Short slotted holes

long slotted holes) (load \perp hole)

$\Rightarrow 0.7$ (long slotted hole) (load \parallel hole)

(7)

μ_f = Slip factor or co-efficient of friction specified in [table-20]. ($\mu_f \leq 0.55$)

Design shear capacity of friction type Bolt

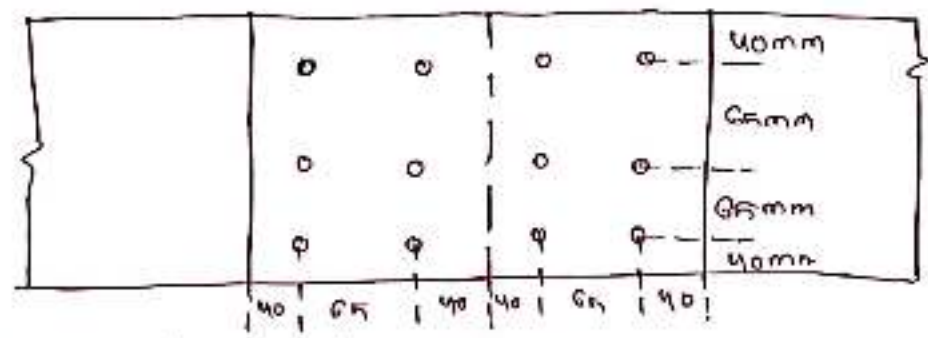
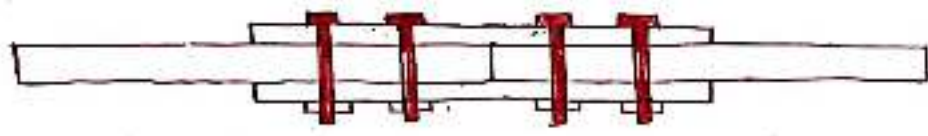
$$V_{df} = \frac{V_{nsf}}{\gamma_{mf}}$$

$\gamma_{mf} \Rightarrow 1.1$ [Service load condition]

$\Rightarrow 1.25$ [Ultimate load condition].

Question

Determine the shear capacity of HSCM Bolts used in connecting two plates are shown in fig.



a-1) Slip resistance designed at Service load

a-2) Slip resistance designed at Ultimate load

- ⇒ Here Bolt of property class 8.8 are used.
- ⇒ fasteners are in clearance holes.
- ⇒ Co-efficient of friction = 0.3.

Data given

$$f_{ub} = 800 \text{ N/mm}^2$$

$$f_{yb} = 800 \times 0.8 = 640 \text{ N/mm}^2$$

$$n_c = 2 \text{ (Double cover butt joint)}$$

$$k_n = 1 \text{ (for fastener clearance holes)}$$

$$\mu_f = 0.3$$

$$P = 65 \text{ mm}$$

$$\Rightarrow P = 2.5 \times d \Rightarrow d = \frac{65}{2.5} = 26 \text{ mm}$$

$$\therefore d = 20 \text{ mm (diameter of bolt)}$$

$$d_o = 20 + 2 = 22 \text{ mm (Pitcher of bolt holes)}$$

$$f_o = \text{proof stress}$$

$$f_o = 0.7 \times f_{ub}$$

$$= 0.7 \times 800 = 560 \text{ N/mm}^2$$

$$\text{Proof Load (T)} = f_o \times A_{nb}$$

Net Area of bolt of threaded portion

$$A_{nb} = 0.78 \times \pi/4 \times d^2$$

$$= 0.78 \times \pi/4 \times 20^2$$

$$= 245.04 \text{ mm}^2$$

$$F_o = f_o \times A_{nb} = 560 \times 245.04 = 137.72 \text{ kN}$$

Nominal shear capacity of bolt

$$V_{nsf} = \mu_F \times k_n \times n_e \times F_o$$

$$= 0.3 \times 1 \times 2 \times 137.72$$

$$= 82.33 \text{ kN}$$

Design slip resistance per bolt

$$V_{dsf} = \frac{V_{nsf}}{\gamma_{mf}}$$

a) Design slip resistance per bolt (for service load cond)

$$V_{dsf} = \frac{82.33}{1.1} = 74.84 \text{ kN}$$

Slip resistance for 6 nos of bolt (V_{dsf}) = 6×74.84

$$= 449.04 \text{ kN}$$

b) $V_{dsf} = \frac{82.33}{1.25}$ (for ultimate load cond)

$$= 65.864 \text{ kN}$$

Slip resistance for 6 nos of bolt (V_{ds}) = $6 \times 65.86 = 395.16 \text{ kN}$

Welded Connection

- * When the steel members are connected with the help of welding then, they are called as welded joint.
- * There are different ways to perform welding
for eg:- Gas welding
Electric Arcs welding ✓
Electric Resistance welding
Seam welding.
- * Generally steel structural elements are joint together with the help of electric arc welding.

Advantages & Disadvantages of welding

Advantages of welding

- * Welding is more adaptable than bolting
- * Self weight of welded structure is less.
- * Welded connection are consider to be rigid.
- * There is no need to drill holes inside member due to which the effective area will become = Gross Area of member.
- * welded joint are strong in case of reversal of stresses.

- * It is possible to achieve 100% of efficiency.
- * Welded connection have good aesthetic appearance
- * Welded connection is air tight and water tight.

Disadvantages of Welded Connection.

- * Welding is effected by the field condition.
- * Skilled person is required to perform welding.
- * Inspection of welded joint is difficult.
- * Residual stresses are present in the welded joint.
- * A welded joint fails earlier than bolted joint because of brittle in nature.

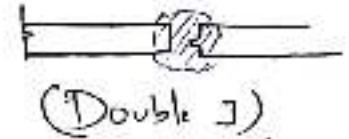
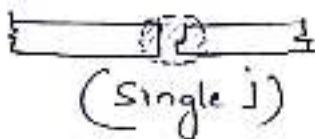
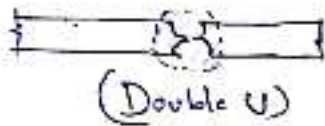
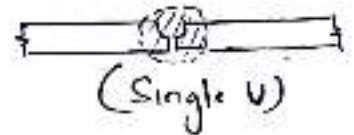
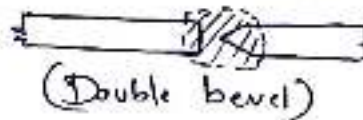
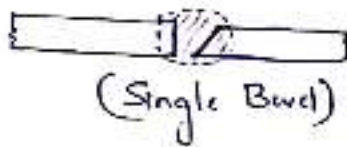
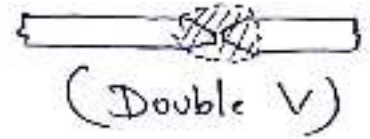
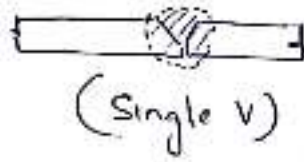
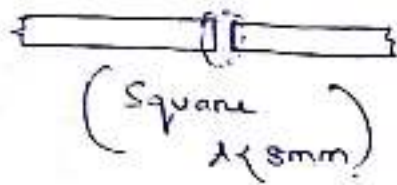
Types of weld

- ① Butt weld
- ② Fillet weld
- ③ Slot weld
- ④ Plug weld

① Butt weld

- * Butt weld are also called as groove weld.
- * Groove weld are provided when the elements to be joint lie in same plane.

If $t > 8\text{mm}$ \rightarrow edge preparation is required
 If $t < 8\text{mm}$ \rightarrow no edge preparation is required, This
 weld is known as square Butt joint.



Assumption in Analysis of Welding

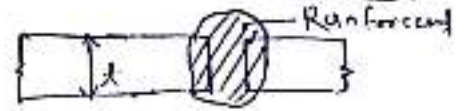
- * Weld material is homogeneous and isotropic.
- * Deformation due to loading will be neglected i.e., welded joint is rigid.
- * Residual stresses are also neglected.
- * Butt weld / groove weld are designed to resist axial tensile / compressive stress.

Notes

fillet weld are design to resist shear stress.

Design Consideration of Butt joint

- * Reinforcement:- extra weld metal above the element surface which increases the size of weld by at least 10%.
- * The maximum size of reinforcement shall not exceed 3mm.



Size of butt weld:-

* It is defined in terms of effective throat thickness (a_e)

* a_e (throat thickness) = $\frac{5}{8} \times t$ (Partial penetration)
throat thickness (a_e) = t (for Double penetration).

Design strength of groove weld.

* Design axial strength of groove weld.

$$P_{dw} = \frac{f_y' \times A_e}{\gamma_{mw}}$$

Design shear strength of butt weld (V_{dw})

$$= \frac{f_y' \times l_w \times a_e}{\sqrt{3} \gamma_{mw}}$$

where,

$\Rightarrow A_e = \text{effective Area} = l_w \times a_e$, $l_w = \text{effective length of butt weld}$;

$\Rightarrow f_y' \rightarrow f_{yw} \rightarrow \text{yield strength of weld metal}$
 $\Rightarrow f_y' \rightarrow f_y \rightarrow \text{yield strength of structural element}$

$a_e = \text{effective throat thickness}$.

(which one is min^m)

$\Rightarrow \gamma_{mw} = \text{partial safety factor for weld material}$

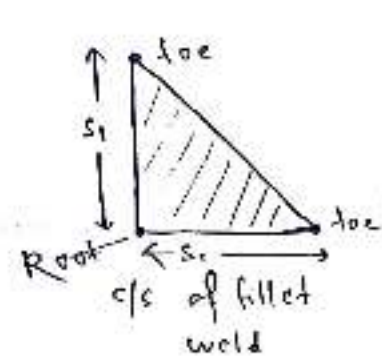
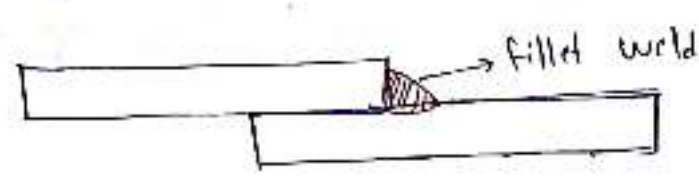
$\gamma_{mw} = 1.25$ for shop weld

$\gamma_{mw} = 1.5$ for field weld

{ IS 800-2007, Pg-30 }
T-5

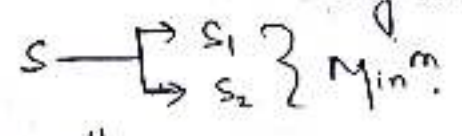
Fillet Weld

- * Fillet weld are designed when the two members to be joined lies in a different plane (there is some inclination between the connecting pieces).
- * Fillet weld are provided when the member to be joined are overlapped with each other.
- * Fillet weld are critical in shear-stress.



Leg size :- It is the distance from the root to toe in the cross section of fillet weld.

Size of weld (S) → It is the min^m of two leg size.

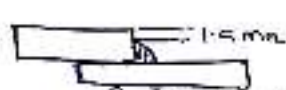


* Minimum size of fillet weld

- * It depends upon thickness of thicker element connected. [IS 800-2007, Pg-78, T-21]
e1 - 10.5.2.3
- * The size of fillet weld shall not be less than 3mm.


Maximum Size of fillet weld

* It depends upon thickness of thinner member connected.

$S_{max} = t - 1.5 \text{ mm}$ → Square edge 

 (IS 800-2007, Pg-79) $\alpha = 10.5.8.1$ (fillet weld on square edges)

$t = \text{thickness of thinner member.}$

$S_{max} = t \times \frac{3}{4}$ → Rounded toe 

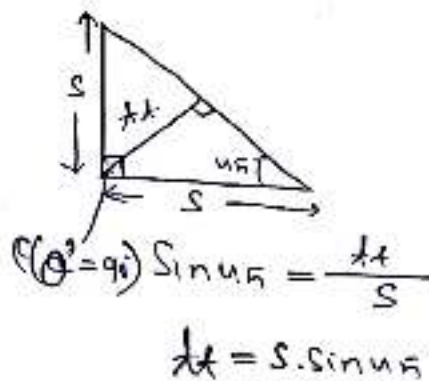
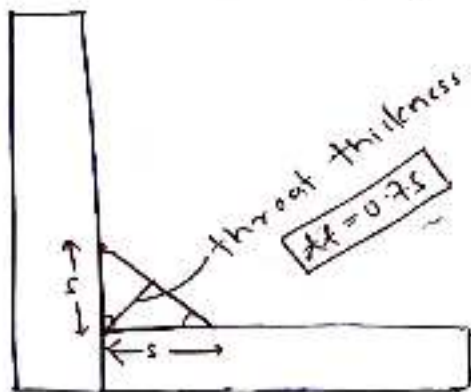
 (Pg-79, $\alpha = 10.5.8.2$) (fillet weld on rounded toe)

$t = \text{thickness of thinner member.}$

effective throat thickness

* It is defined as the minimum dimension in the cross-section of fillet weld.

* Throat thickness shall not be less than 3mm.



* Throat thickness depends upon angle of inclination θ
 eg. If $\theta = 90^\circ$, $t_t = 0.7s$

In general $t_t = ks$ (IS 800-2007, Pg-78) $T-22$

$\therefore k = \text{constant which depends upon angle of inclination}$

* effective length of fillet weld L_w

(IS 800-2007, Pg-78)
Cl- 10.5.4.1

$$L_w = L - 2 \times \text{Size of weld}$$

L_w = effective length of weld.

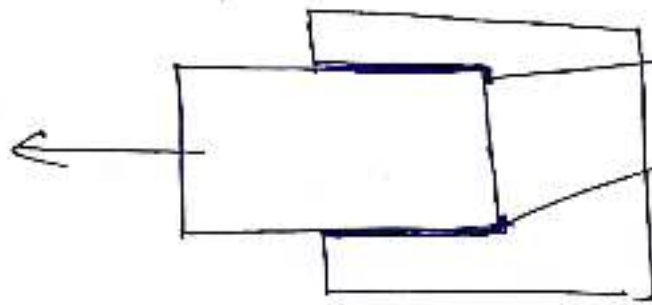
L = overall length of weld

* effective length of weld shall never be less than $4 \times S$

S = size of weld

$$L_w = 4 \times S$$

End Return



end Return

end return should not be less than $2 \times \text{Size of weld}$.

Designe strength of fillet weld

Designe stress in fillet weld, $f_{wd} = \frac{f_{tw}}{\gamma_{mw}}$

f_{tw} = nominal stress in fillet weld.

γ_{mw} = partial safety factor.

$\gamma_{mw} = 1.25$ for shop weld (IS 800-2007, Pg-30)
 $\gamma_{mw} = 1.5$ for field weld (T-5)

Designe strength of fillet weld = Designe stress $\times A_e$

$$= \frac{f_{tw}}{\gamma_{mw}} \times A_e$$

$$P_{qw} = \frac{f_{rw}}{r_{mw}} \times A_e$$

$$= \frac{f_u'}{\sqrt{3} r_{mw}} \times (L_w \times t_e)$$

$$P_{qw} = \frac{f_u'}{\sqrt{3} r_{mw}} \times L_w \times t_e$$

$$f_u' \rightarrow \left. \begin{array}{l} \rightarrow f_{uw} \\ \rightarrow f_u \end{array} \right\} \text{min.}$$

f_{uw} = ultimate strength of weld metal

f_u = ultimate strength of element.

If load is given, then for a particular size of weld, the length of weld required will be:

$$P_u = P_{qw} = \frac{f_u'}{\sqrt{3} r_{mw}} \times (L_w \times t_e)$$

$$L_w = \frac{P_u \times \sqrt{3} \times r_{mw}}{f_u' \times k \times s}$$

Question-1

A 15 mm thick plate is joint to a 16mm plate by 200 mm long (effective) butt welded determine the strength of joint.

If

- 1) A double V butt weld is used.
- 2) A single V butt weld is used.

Assume Fe410 grade plate and shop welded are used.

Data given

$f_u = 410 \text{ N/mm}^2$

$f_y = 250 \text{ N/mm}^2$

$L_w = 200 \text{ mm}$ (effective length of weld)

$\gamma_{mw} = 1.25$ (shop weld).

thickness of thinner plate (t) = 16 mm.

double V butt weld

Throat thickness (a_t) = (t) thickness of thinner plate.
 = 16 mm (fully penetration)

Design strength of weld (P_{dw}) = $\frac{f_y' \times L_w \times a_t}{\gamma_{mw}}$

$\rightarrow f_y' = f_y = 250 \text{ N/mm}^2$

$$= \frac{250 \times 200 \times 16}{1.25}$$

$$= 640 \text{ kN.}$$

Single V butt weld

$$\begin{aligned} \text{Throat thickness } (t_e) &= \frac{5}{8} \times l \quad (\text{partially penetration}) \\ &= \frac{5}{8} \times 16 = 20 \text{ mm} \end{aligned}$$

Design strength of butt weld

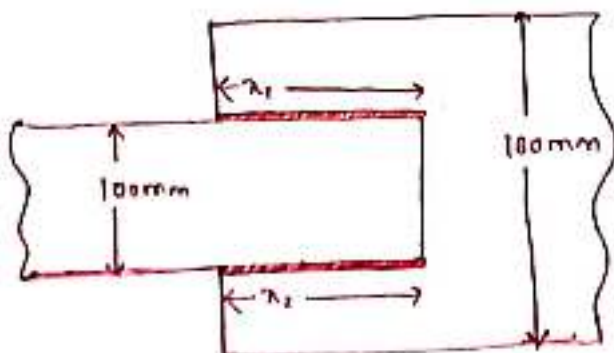
$$P_d = \frac{f_y' \times l_w \times t_e}{\gamma_{mw}}$$

$$= \frac{250 \times 200 \times 10}{1.25}$$

$$= 400 \text{ kN}$$

Question - 3

Design a suitable longitudinal fillet weld to connect the plates as shown in fig, to transmit a pull equal to the full strength of small plate, given plates 10mm thick, grade of plate Fe410 and welding should be made in workshop.



Data given

$$f_u = 410 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

$$\gamma_{mw} = 1.25 \text{ (work show writing)}$$

thickness of plate $t = 12 \text{ mm}$

Minimum size of weld (s_{min}) = 5 mm [IS 800-2007, Pg-28]
T-21

Maximum size of weld (s_{max}) = $12 \cdot 1.5 = 10.5 \text{ mm}$ (Square edge)

\therefore Size of weld $(s) = 10 \text{ mm}$ (Assume).

Gross Area of small plate (A_g) = $B \times t = 100 \times 12 = 1200 \text{ mm}^2$

$$\text{Strength of solid plate } (T_g) = \frac{A_g \times f_y}{\gamma_{ms}}$$

$$= \frac{1200 \times 250}{1.1}$$

$$= 272.72 \text{ kN.}$$

Throat thickness of fillet weld (t_e) = $k_s \cdot s$ ($\theta = 90^\circ$)
= $0.7 \times 10 = 7 \text{ mm}$

$$\text{Strength of fillet weld} = \frac{f_u' \times l_w \times t_e}{\sqrt{3} \times \gamma_{mw}}$$

$$= \frac{410 \times l_w \times 7}{\sqrt{3} \times 1.25}$$

$$= 1.32 l_w \text{ kN}$$

Design strength of weld = strength of solid plate

$$\Rightarrow 1.33 \times lw = 272.72$$

$$\Rightarrow w = \frac{272.72}{1.33} = 205.05 \text{ mm} \approx 210 \text{ mm}$$

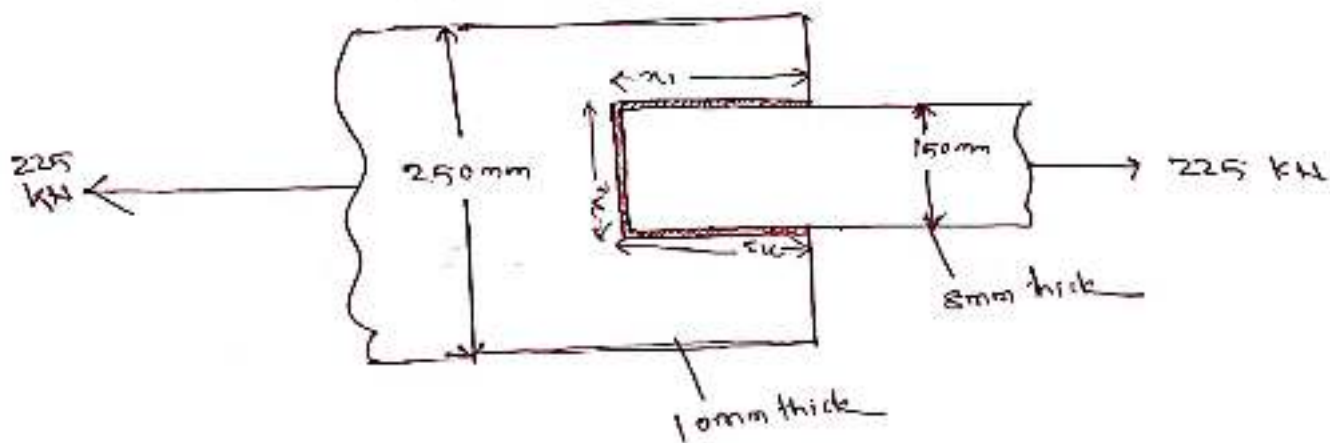
\therefore effective length of weld $w = 210 \text{ mm}$

$$x_1 + x_2 = 210 \text{ mm} \quad (x_1 = x_2)$$

$$x_1 = x_2 = \frac{210}{2} = 105 \text{ mm} \quad \underline{\text{Ans}}$$

Assignment

Design a suitable fillet weld to connect two plate as shown in below use Fe410 grade of plate is used.



$$x_1 = ?$$
$$x_2 = ?$$
$$x_3 = ?$$

Data given

$$f_u = 410 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

thickness of thinner plate = 8 mm

thickness of thicker plate = 10 mm

(2h)
Minimum size of weld (S_{min}) = 3 mm (IS 800-2007, Pg-78)

Maximum size of full weld (S_{max}) = $8 - 1.5$ T-21

(Size of weld) $\therefore S = 6$ mm = 6.5 mm (Square edge).

effective throat thickness (t_e) = $k \times S$ ($\theta = 90^\circ$)
 $= 0.7 \times 6 = 4.2$ mm

Tensile load = 225 kN

\Rightarrow Design strength of weld = $\frac{L_w \times t_e \times f_u}{\sqrt{3} \times \gamma_{mw}}$

\Rightarrow ($\gamma_{mw} = 1.25$
As per IS 800:2007)

$$= \frac{L_w \times 4.2 \times 410}{\sqrt{3} \times 1.25}$$
$$= L_w \times 0.795 \text{ kN}$$

\Rightarrow Design strength of weld = Tensile load (Design purpose)

$\Rightarrow L_w \times 0.795 = 225$

$\Rightarrow L_w = \frac{225}{0.795} = 283.01 \text{ mm} \approx 290 \text{ mm}$

\therefore effective length of weld $L_w = 290 \text{ mm}$

$$x_1 + x_2 + x_3 = 290 \text{ mm}$$

$$x_2 = 150 \text{ mm}$$

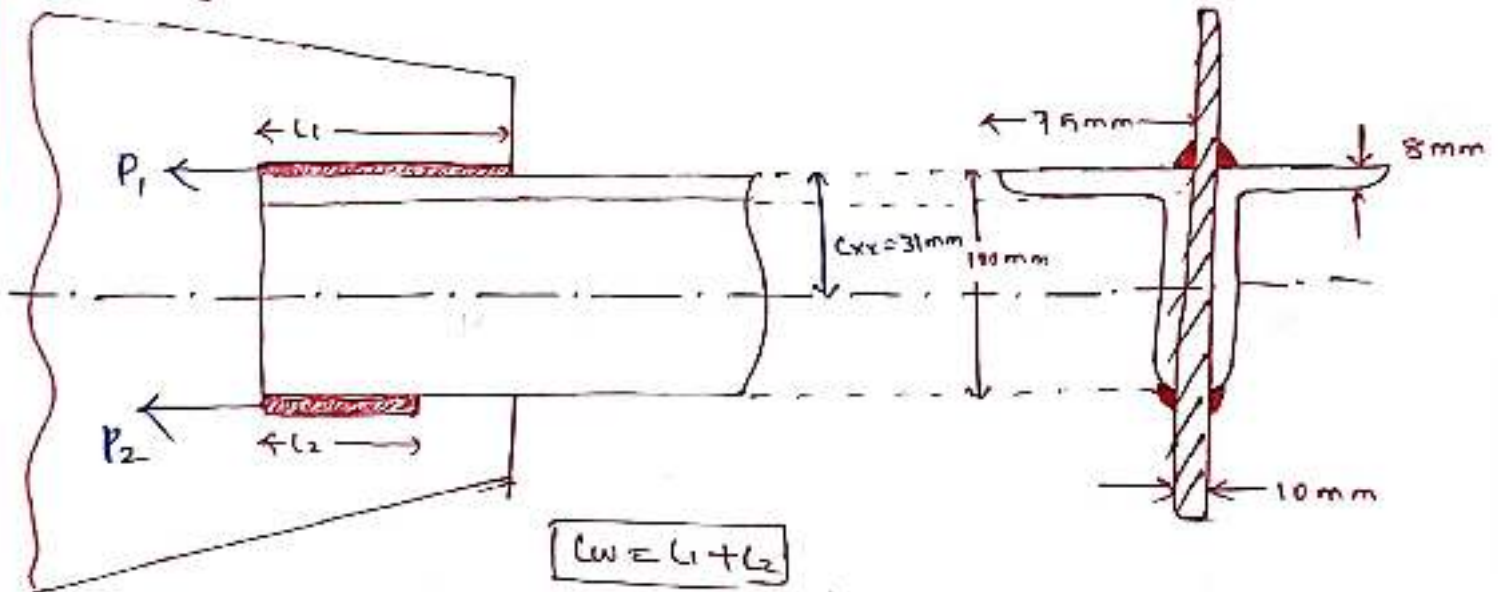
$$x_1 = x_3 = \frac{290 - 150}{2} = 70 \text{ mm}$$

Ans

Question

A tie member of a roof truss consists of ISA 100 x 75 x 8 mm. The angle are completely within side of a 100 mm gusset plate and the member is subjected to a working pull of 300 kN.

Design the welded connection assume the connection are made in workshop. Fe410 grade plate are used.



Data given

$$f_u = 410 \text{ N/mm}^2$$

$$\text{Working pull} = 300 \text{ kN}$$

$$\text{Factored load/pull} = 300 \times 1.5 = 450 \text{ kN}$$

$$\text{Factored load per one angle} = 450 / 2 = 225 \text{ kN}$$

$$\sigma_{tw} = 125 \text{ (shop weld)}$$

$$l_{min} = 8 \text{ mm}, l_{max} = 10 \text{ mm}$$

$$\text{Minimum size of weld (Smin)} = 3 \text{ mm} \quad \cdot \quad (T-21, P_3-75)$$

26

$$\text{Maximum size of weld } (S_{\max}) = \frac{3}{4} \times t \quad (\text{Round shape edge})$$

$$= \frac{3}{4} \times 8 = 6 \text{ mm}$$

$$\therefore S = 6 \text{ mm}$$

$$\text{effective throat thickness } (t_e) = k \times S \quad (\theta = 90^\circ)$$

$$= 0.7 \times 6 = 4.2 \text{ mm}$$

$$\text{Design strength of weld } (P_d) = \frac{f_u \times L_w \times t_e}{\sqrt{3} \times \gamma_{mw}}$$

$$= \frac{410 \times L_w \times 4.2}{\sqrt{3} \times 1.25}$$

$$= 0.795 \times L_w \text{ kN.}$$

\therefore Design strength of weld = Factored load

$$\Rightarrow 0.795 \times L_w = 225 \text{ kN}$$

$$\Rightarrow L_w = \frac{225}{0.795} = 283.01 \text{ mm} \geq 290 \text{ mm.}$$

$$\therefore L_w = 290 \text{ mm.}$$

CG of Angle $C_{xx} = 31 \text{ mm}$ (Steel table, pg-14)
ISA

taking Moment about CG.

$$P_1 \times C_{xx} = P_2 \times (100 - C_{xx})$$

$$\Rightarrow \frac{f_u \times L_w \times t_e}{\sqrt{3} \times \gamma_{mw}} \times C_{xx} = \frac{f_u \times L_w \times t_e}{\sqrt{3} \times \gamma_{mw}} \times (100 - C_{xx})$$

$$\Rightarrow l_1 \times 31 = l_2 \times (100 - 31)$$

$$\Rightarrow l_1 = l_2 \times \left(\frac{100 - 31}{31} \right)$$

$$\boxed{l_1 = 2.72 l_2}$$

$$l_0 = l_1 + l_2$$

$$\Rightarrow 290 = \cancel{90} + 2.72 l_2 + l_2$$

$$\Rightarrow l_2 = \frac{290}{3.22} = 90 \text{ mm}$$

$$\Rightarrow l_1 = 290 - 90 = 200 \text{ mm}$$

Ans

Design of Tension Member.

- * A structural element which is subjected to two pulling forces at its end are called tension member.

Types of Section member

- 1) Cables :-
- * They are ideal tension members because, they can not resist compression and bending stress.
 - * They are made from multiple wires which are helically rounded.
 - * They are used in suspension bridge.

- 2) Flat or plates :- In plate, bolting can be done in a way that the cut of member coincide with the cut of connection which no bending effect are generated.
- * In case of compression ~~member~~ applied to flat or plates they will fail easily, because they have less radius of gyration.
 - * They can be used in lacing or battening.

3) Angle or Builtup Section

- * For a given area angle section provides more stiffness as compared to flat sections.
- * Angle section can be connected either with bolting or welding.

- * In case of heavy loading builtup section on I-section is used as a tension member.

4) Hollow Section

- * In addition to tensile strength hollow section have good compressive strength therefore they are used as Bracing element.
- * Hollow section are generally connected with the help of welding.

Failure of tension Member

- * failure of tension member is governed by two limit state

1) Yielding failure

2) Rupture/fracture failure

- * There are 3 modes in which these limit state could be reached.

① Gross section yielding

- * Due to gross section yielding the member deforms to a very large value due to which the member becomes unserviceable, Hence it will fail in limit state of serviceability.

② Net Section Rupture

- * When ultimate stress are reached at the net section the rupture take place in the connecting element through the bolt holes.

2

③ Block shear failure

* In this failure a segment of member get cutted out from the joint. In this failure shear occurs at one plane and tension occurs at adjacent plane.

Design strength of Tension Member.

* It depends upon the following strength's criteria

① Design strength in Gross section yielding

(IS 800-2007, Pg-32, CL-6.2)

$$T_{dg} = \frac{A_g \times f_y}{\gamma_{m0}}$$

f_y = yield strength of member.

A_g = Gross sectional Area

γ_{m0} = Partial Safety factor (1.5 - Pg-30 > T-5)

② Design strength of Tension member due to net section

Rupture:-

(IS 800-2007, Pg-32)
CL-6.3

a) Flat & Plate

$$T_{dn} = \frac{0.9 \times A_n \times f_u}{\gamma_{m1}}$$

Where,

f_u = Ultimate strength of member.

γ_{m1} = partial safety factor = 1.25 (Pg-50, T-5)

A_n = Net Sectional Area.

$A_n = (B - n d_o) \times t$ (for chain bolting)

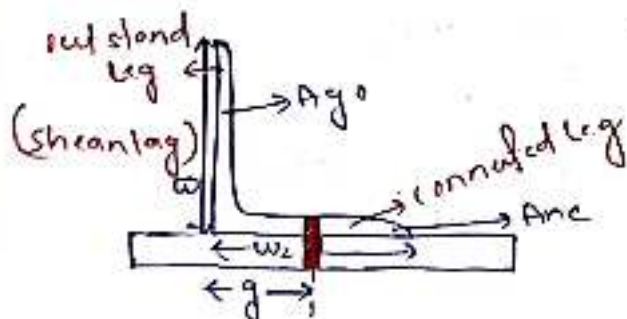
$A_n = \left[B - n d_o + \sum_{i=1}^{m-1} \frac{p_s^2}{4g_i} \right] \times t$ (for staggered bolting)



b) Angle Section

* In case of angle section connected with one leg only with gusset plate. The out standing leg will be effected by shear lag.

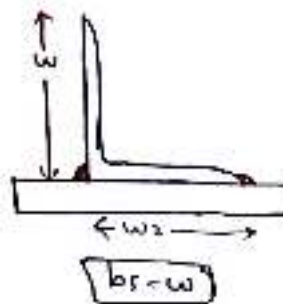
$$T_d = \frac{0.9 \times f_u \times A_{nc}}{\gamma_{m1}} + \frac{A_{go} \times f_y}{\gamma_{m0}} \times \beta$$



$$b_s = w + g - t$$

$$A_{go} = (w - t/2) \times t$$

$$A_{nc} = (w_2 - t/2 - n d_o) \times t$$



$$A_{go} = (w - t/2) \times t$$

$$A_{nc} = (w_2 - t/2) \times t$$

②

where,

$$\beta = 1.4 - 0.076 \left(\frac{w}{t} \right) \times \left(\frac{f_y}{f_u} \right) \times \left(\frac{b_s}{l_c} \right) \leq \left(\frac{f_u \gamma_{m0}}{f_y \gamma_{m1}} \right) \geq 0.7$$

A_{nc} = Net sectional area of connected leg.

A_{go} = Gross sectional area of outstanding leg.

w = width of outstanding leg.

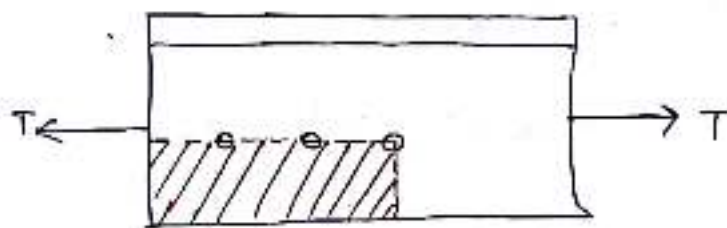
t = thickness of element

b_s = Distance from tip of out standing leg to the center of first bolt line.

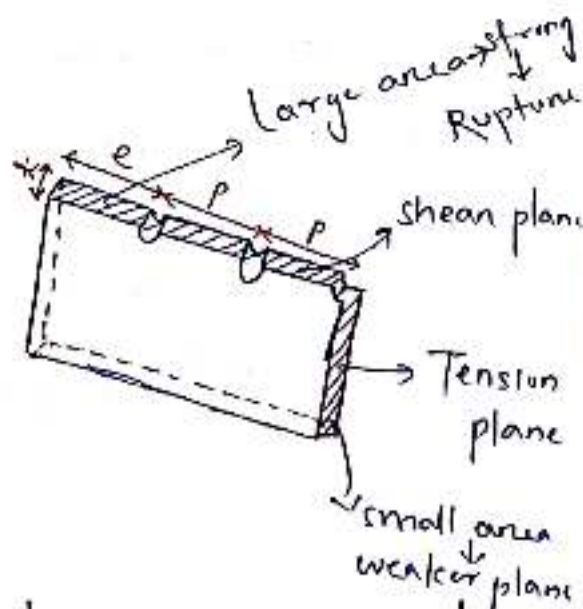
l_c = Length of connection.

③ Design strength in Block Shear

* The Block shear failure occurs due to combined effect of shear ~~one~~ one plane and tension on the other plane.



shaded area will tear out from member.



\therefore Block shear strength = Rupture strength of stronger plane + Yield strength of weaker plane.

[IS 800-2007, Pg-33, Cl-6.4]

Case-1

Rupture of shear plane + Yielding of tension plane

$$T_{db1} = \frac{0.9 f_u \times A_{vn}}{\sqrt{3} \times \gamma_{m1}} + \frac{f_y \times A_{tg}}{\gamma_{m0}}$$

Case-2

Rupture of tension plane + Yielding of shear plane

$$T_{db2} = \frac{0.9 \times f_u \times A_{tn}}{\gamma_{m1}} + \frac{f_y \times A_{vg}}{\sqrt{3} \times \gamma_{m0}}$$

where

$A_{vg} \rightarrow$ Gross area in shear = $(e + 2p) \times t$: (from figure)

$A_{vn} \rightarrow$ Net area in shear = $(e + 2p - 2.5 \times d_o) \times t$

$A_{tg} \rightarrow$ Gross area in tension = $e \times t$

$A_{tn} \rightarrow$ Net area in tension = $(e - 0.5 \times d_o) \times t$

Design strength of tension in Block shear

$$= \min(T_{db1}, T_{db2})$$

\therefore Design strength of tension member as per limit state

$$T_{min} \left\{ \begin{array}{l} T_{dg} \\ T_{dn} \\ T_{db} \end{array} \right.$$

Check for Slenderness Ratio

Slenderness ratio for tension member is defined as the ratio of unsupported length of the member to its least radius of gyration.

$$\lambda = \frac{L_e}{r_{min}}$$

L_e = unsupported length

r_{min} = least radius of gyration

$$r_{min} = \sqrt{\frac{I_{min}}{A}}$$

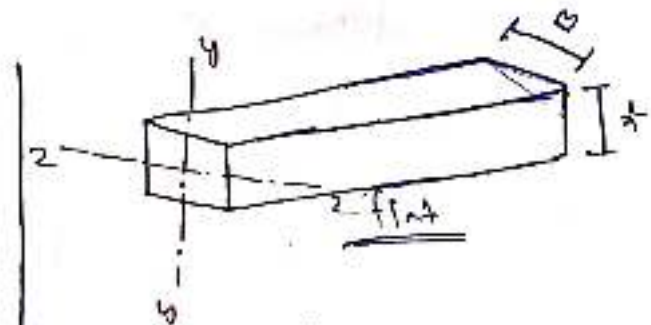
$$I_{min} = A r_{min}^2$$

I = moment of inertia

A = Area of section

IS 800-2007 has kept a restriction over the slenderness ratio of the tension member subjected to reversal of stress

[IS 800-2007 Pg-20, T-3]



$$\left. \begin{aligned} I_{zz} &= \frac{B t^3}{12} \\ I_{yy} &= \frac{t \times B^3}{12} \end{aligned} \right\} I_{zz} = \min$$

$$r_{min} = \sqrt{\frac{\frac{B t^3}{12}}{B \times t}} = \frac{t}{\sqrt{12}}$$

Member	Maximum effective Slenderness Ratio
① A tension member in which reversal of direct stress occurs due to loads other than wind & seismic loading (DL+LL)	180
② A member normally acting as a tie in roof truss over a bracing system but subjected to possible of reversal stress resulting from action of wind on earthquake	350

③ for any other tension member

400.

(Other than prestressed members)

Design procedure (Limit state)

given \Rightarrow Applied load, 'T' $\Rightarrow T_u = \gamma_f \times T$ (Applied factored load)

Step-1 \rightarrow Determine the required area of cross-section

$$T_u = T_d \leq \frac{A_g \times f_y}{\gamma_{mo}}$$

$$A_g = \frac{T_u \times \gamma_{mo}}{f_y}$$

Note

\therefore (A_g increasing by 25%)

Step-2 \rightarrow From IS Hand book no. 1 select a Rolled steel section of a particular shape which provides the gross area equals to or greater than the required gross area.

Step-3 \rightarrow Design of connection.

Bolting

* Diameter of bolt = $0.04 \sqrt{A}$

* Strength of Bolt $\rightarrow B_v$

* No of bolt (n) $\rightarrow \frac{P_u}{B_v}$

* Arrange the bolts suitably into the members.

Step-4 \rightarrow Determine the Design tensile strength of the member (T_d)

i) Gross section yielding strength (T_{dy})

ii) Net section rupture strength (T_{dn})

iii) Block shear strength (T_{db})

min^m = T_d

$$T_d \geq T_u$$

safe

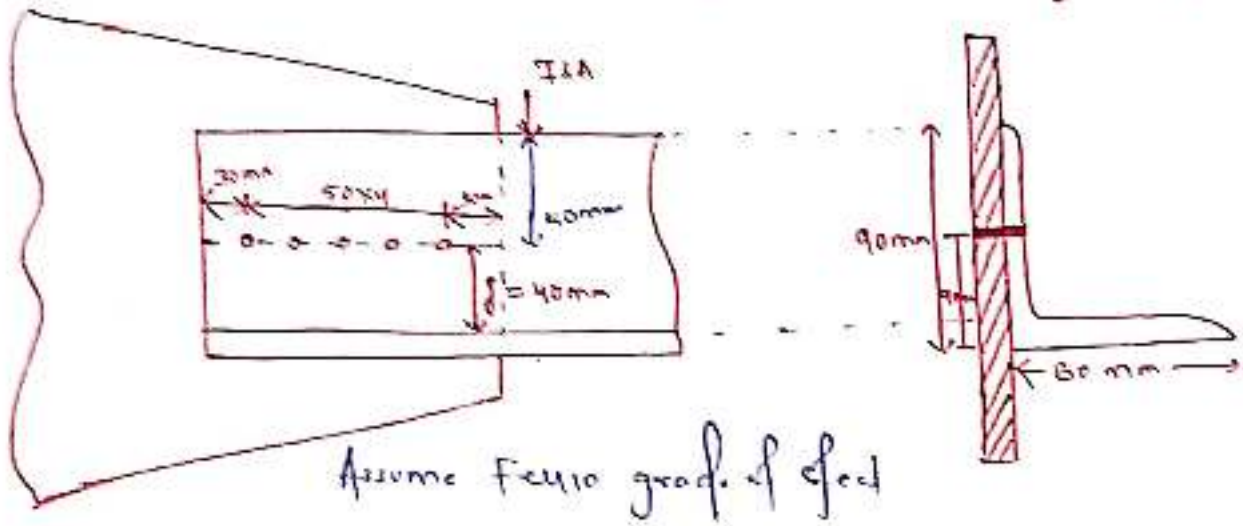
Step-5 \rightarrow Check for slenderness Ratio :-

$\lambda_{\text{member}} \neq \lambda_{\text{max}}$ (Give IS code)

5

Question-1

A single unequal angle ISA 90x60x6 mm is connected to a 10 mm gusset plate at the end with a row of 16 mm bolts to transfer tension determine the design tensile strength of the angle if 90 mm leg is connected to gusset plate.



Data given

$f_y \rightarrow 250 \text{ mpa}$, $d = 16 \text{ mm}$
 $f_u = 410 \text{ N/mm}^2$, $d_0 = 16 + 2 = 18 \text{ mm}$

① Gross section yielding strength

$$T_{dg} = \frac{f_y \times A_g}{\gamma_{mo}} \quad (\gamma_{mo} = 1.1)$$

A_g = gross area of plate Angle section

$A_g = 8.65 \text{ cm}^2 \approx 865 \text{ mm}^2$ (from steel table)
Pg-14

$$T_{dg} = \frac{250 \times 865}{1.1} = 196.59 \text{ kN}$$

② Net Section Rupture strength

$$T_{dn} = \frac{0.9 \times f_u \times A_{nc}}{\gamma_{m1}} + \frac{A_{g0} \times f_y}{\gamma_{m0}} \times \beta$$

A_{nc} = Area of connected leg

$$\begin{aligned} A_{nc} &= (90 - t/2 - r_{d0}) \times t \\ &= (90 - 6/2 - 18) \times 6 \\ &= 414 \text{ mm}^2 \end{aligned}$$

A_{g0} = Area of out stand leg.

$$\begin{aligned} A_{g0} &= (60 - t/2) \times t \\ &= (60 - 6/2) \times 6 \\ &= 342 \text{ mm}^2 \end{aligned}$$

$$\beta = 1.4 - 0.076 \times \frac{w}{t} \times \frac{f_y}{f_u} \times \frac{b_s}{L_c}$$

$$w = \text{length of out stand leg} = 60 \text{ mm}$$

$$t = 6 \text{ mm}$$

$$\begin{aligned} b_s &= w + g - t = 60 + 40 - 6 \\ &= 94 \text{ mm} \end{aligned}$$

$$L_c = 50 \times 4 = 200 \text{ mm}$$

$$\begin{aligned} \Rightarrow \beta &= 1.4 - 0.076 \times \frac{60}{6} \times \frac{250}{410} \times \frac{94}{200} \\ &= 1.18 \end{aligned}$$

Check $\frac{f_u \gamma_{m0}}{f_y \gamma_{m1}} = \frac{410 \times 1.1}{250 \times 1.25} = 1.44 \geq 1.18$

$$0.7 \leq 1.18$$

$$\therefore \beta = 1.18$$

6

$$T_d = \frac{0.9 \times 410 \times 414}{1.25} + \frac{342 \times 250 \times 1.18}{1.1}$$

$$= 213.93 \text{ kN}$$

③ Block Shear strength

~~T_{db1}~~

$$A_{vn} = (e + 4xp - 4.5d_0) \times t = (30 + 4 \times 50 - 4.5 \times 18) \times 6 = 894 \text{ mm}^2$$

$$A_{vg} = (e + 4xp) \times t = (30 + 4 \times 50) \times 6 = 1380 \text{ mm}^2$$

$$A_{tg} = 50 \times t = 50 \times 6 = 300 \text{ mm}^2$$

$$A_{tn} = (50 - 0.5 \times d_0) \times t = (50 - 0.5 \times 18) \times 6 = 246 \text{ mm}^2$$

$$T_{db1} = \frac{0.9 \times f_u \times A_{tn}}{\gamma_{m1}} + \frac{f_y \times A_{vg}}{\sqrt{3} \times \gamma_{m0}}$$

$$= \frac{0.9 \times 410 \times 246}{1.25} + \frac{250 \times 1380}{\sqrt{3} \times 1.1}$$

$$= 253.69 \text{ kN}$$

$$T_{db2} = \frac{0.9 \times f_u \times A_{vn}}{\sqrt{3} \times \gamma_{m1}} + \frac{A_{tg} \times f_y}{\gamma_{m0}}$$

$$= \frac{0.9 \times 410 \times 894}{\sqrt{3} \times 1.25} + \frac{300 \times 250}{1.1}$$

$$= 220.54 \text{ kN}$$

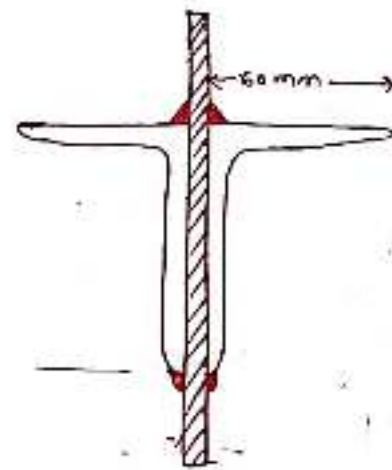
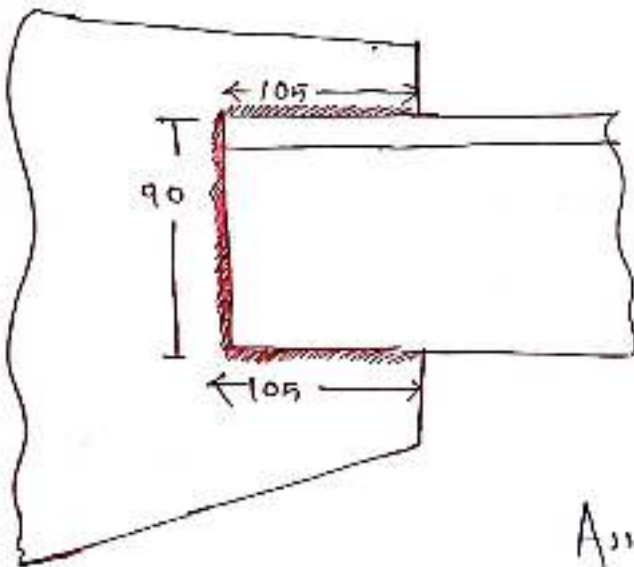
$$\therefore T_{db} = \min^m (T_{db1}, T_{db2})$$

$$T_{db} = 220.54 \text{ kN}$$

\therefore Design tensile strength of tension member = $\min^m (196.59 \text{ kN}, 213.93 \text{ kN}, 220.54 \text{ kN})$
 $\therefore T_d = 196.59 \text{ kN}$

Question-2

Determine the tensile strength of a roof truss member
2 ISA 90x60x6mm² connected to the gusset plate
of 8mm thickness by 4mm weld as shown in fig.
The effective length of the weld is 300mm.



Assume Fe250 grade of steel

Data given

ISA 90x60x6mm

$$f_u = 410 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

Thickness of gusset plate = 8mm.

Size of weld = 4mm

effective length of weld = 300mm.

$$\begin{aligned} \text{Area of connected leg (A}_{nc}) &= (90 - t/2) \times t \times 2 \quad \rightarrow 2 \text{ angles?} \\ &= (90 - 6/2) \times 6 \times 2 \\ &= 1044 \text{ mm}^2. \end{aligned}$$

7

$$\begin{aligned} \text{Area of out standing leg} &= (60 - t/2) \times t \times 2 \\ &= (60 - 6/2) \times 6 \times 2 \\ &= 684 \text{ mm}^2. \end{aligned}$$

$$\begin{aligned} \text{Gross Area } (A_g) &= 865 \text{ cm}^2 \text{ (from steel table)} \\ &= 865 \text{ mm}^2 \times 2 = 1730 \text{ mm}^2 \end{aligned}$$

① Gross Yielding strength

$$\begin{aligned} T_{dy} &= \frac{f_y \times A_g}{\gamma_{mo}} \\ &= \frac{250 \times 1730}{1.1} \\ &= 393.18 \text{ KN.} \end{aligned}$$

② Design strength due to Net Rupture

$$\begin{aligned} T_{dn} &= \frac{0.9 \times f_u \times A_{nc}}{\gamma_{m1}} + \frac{\beta \times f_y \times A_{go}}{\gamma_{m0}} \\ &= \frac{0.9 \times 410 \times 1044}{1.25} + \frac{\beta \times 250 \times 684}{1.1} \end{aligned}$$

$$\beta = 1.4 - 0.076 \times \left(\frac{w}{t}\right) \times \left(\frac{f_y}{f_u}\right) \times \left(\frac{b_s}{L_c}\right)$$

$$\begin{aligned} w &= 60 \text{ mm}, L_c = 105 \text{ mm} = \left(\frac{105 + 105}{2}\right) \\ t &= 6 \text{ mm}, b_s = 60 \text{ mm} \end{aligned}$$

$$\beta = 1.4 - 0.076 \times \left(\frac{60}{6}\right) \times \left(\frac{250}{410}\right) \times \left(\frac{60}{105}\right)$$

$$= 1.13$$

check

$$\frac{f_u \times \gamma_{m0}}{f_y \times \gamma_{m1}} = \frac{410 \times 1.1}{250 \times 1.25} = 1.44 \geq 1.13$$

$$0.7 \leq 1.13 \text{ (ok)}$$

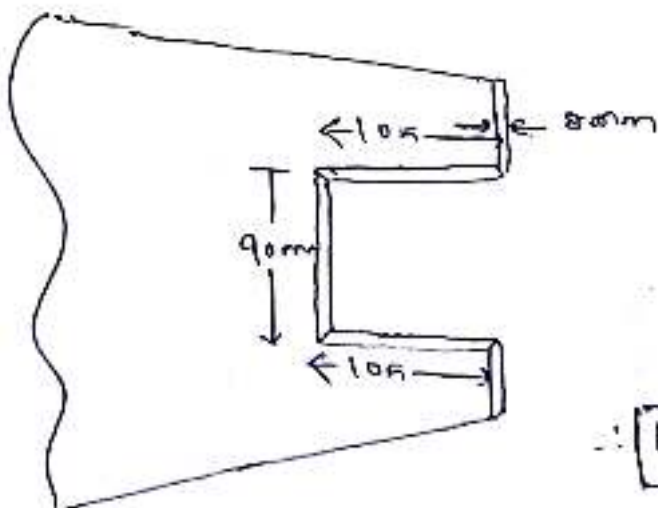
$$\therefore \beta = 1.13$$

$$T_d = \frac{0.9 \times 410 \times 1044}{1.25} + \frac{1.13 \times 250 \times 684}{1.1}$$

$$= 483.85 \text{ kN}$$

③ Block shear strength

* In the case of welding block shear failure mainly occurs in gusset plate, so, we determined the block shear strength of gusset plate. up thickness



$$A_{vn} = A_{vg} = \left(\frac{105 + 105}{2}\right) \times 8 \times 2$$

$$= 1680 \text{ mm}^2$$

$$A_{tg} = A_{tn} = 90 \times 8 = 720 \text{ mm}^2$$

$$\therefore A_{vn} = A_{vg} = 2 \times L_c \times t \text{ (up)}$$

$$\begin{aligned}
 T_{db1} &= \frac{0.9 \times A_{tn} \times f_u}{\gamma_{m1}} + \frac{f_y \times A_{vg}}{\sqrt{3} \times \gamma_{m0}} \\
 &= \frac{0.9 \times 220 \times 410}{1.25} + \frac{250 \times 1680}{\sqrt{3} \times 1.1} \\
 &= 432.98 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 T_{db2} &= \frac{0.9 \times f_u \times A_{vn}}{\sqrt{3} \times \gamma_{m1}} + \frac{f_y \times A_{tg}}{\gamma_{m0}} \\
 &= \frac{0.9 \times 410 \times 1680}{\sqrt{3} \times 1.25} + \frac{250 \times 220}{1.1} \\
 &= 449.96 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 \therefore T_{db} &= \min^m (T_{db1}, T_{db2}) \\
 &= (T_{db} = 432.98 \text{ kN})
 \end{aligned}$$

\therefore Design Tensile strength of tension member

$$T_d = \min^m (T_{dg}, T_{dn}, T_{db})$$

$$= \min^m (393.18, 483.85 \text{ kN}, 432.98)$$

$$\therefore (T_d = 393.18 \text{ kN})$$

Ans

Design problem

Design a single angle section for a tension member of a roof truss to carry a factored tensile force of 225 kN. The member is subjected to the possible reversal stress due to the action of ~~low~~ wind. The effective length of the member is 3m. Use 20 mm shop bolts of grade 4.6 for the connection.

Data given

Factored load (T_u) = 225 kN.

Effective length = 3m

Diameter of bolt (d) = 20mm

Diameter of bolt holes (d_0) = 20 + 2 mm.

$$f_{yb} = 400 \times 0.6 = 240 \text{ N/mm}^2$$

$$f_{ub} = 400 \text{ N/mm}^2$$

Assume Fe410 grade of member

$$f_y = 250 \text{ N/mm}^2$$

$$f_u = 410 \text{ N/mm}^2$$

Step-1 Gross Area of tension member

$$\begin{aligned} A_g &= \frac{T_u \times \gamma_{mo}}{f_y} \\ &= \frac{225 \times 10^3 \times 1.1}{250} = 990 \text{ mm}^2. \end{aligned}$$

(9)

A_g increase by 25%. (generally 25-40%) Increase

$$A_g = 990 \times 1.25 = 1237.5 \text{ mm}^2$$

Step 2

* Try ISA 10075 x 8 mm

$$A_g = 1336 \text{ mm}^2 \quad (\text{from steel table})$$

pg-14

Step 3 Design of Connection

* Bolt strength

$$d = 20 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

$$e = 1.5 \times d_o = 1.5 \times 22 = 33 \pm 40 \text{ mm}$$

$$p = 2.5 \times d = 2.5 \times 20 = 50 \text{ mm} \leq 60 \text{ mm}$$

① Design Shear strength of a Bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} [n_s \times A_{sb} + n_n \times A_{nb}]$$

1 Single shear $n_s = 0, n_n = 1$

$$\text{Area of bolt at shank } (A_{sb}) = \frac{\pi}{4} \times 20^2 = 314.159 \text{ mm}^2$$

$$\text{Area of thread portion } (A_{nb}) = 0.78 \times A_{sb} = 0.78 \times 314.159 = 245.044 \text{ mm}^2$$

$$V_{dsb} = \frac{400}{\sqrt{3} \times 1.25} \times [1 \times 245.044]$$

$$= 45.272 \text{ kN}$$

② Design Bearing strength of a Bolt

$$V_{dpb} = \frac{2.5 \times k_b \times d \times t \times f_u}{\gamma_{mb}}$$

$$t = 8 \text{ mm}, d = 20 \text{ mm}, f_u = 410 \text{ N/mm}^2$$

$\Rightarrow k_b = \text{Bearing factor}$

$$\Rightarrow \frac{e}{3d_0} = \frac{40}{3 \times 22} = 0.6$$

$$\Rightarrow \frac{P}{3d_0} - 0.25 = \frac{60}{3 \times 22} - 0.25 = 0.65$$

$$\Rightarrow \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$\Rightarrow 1$

~~∴~~ $\therefore k_b = 0.6$

$$V_{dpb} = \frac{2.5 \times 0.6 \times 20 \times 8 \times 410}{1.25}$$

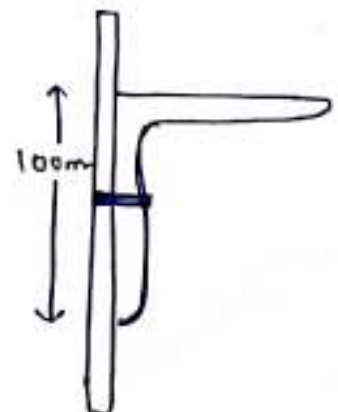
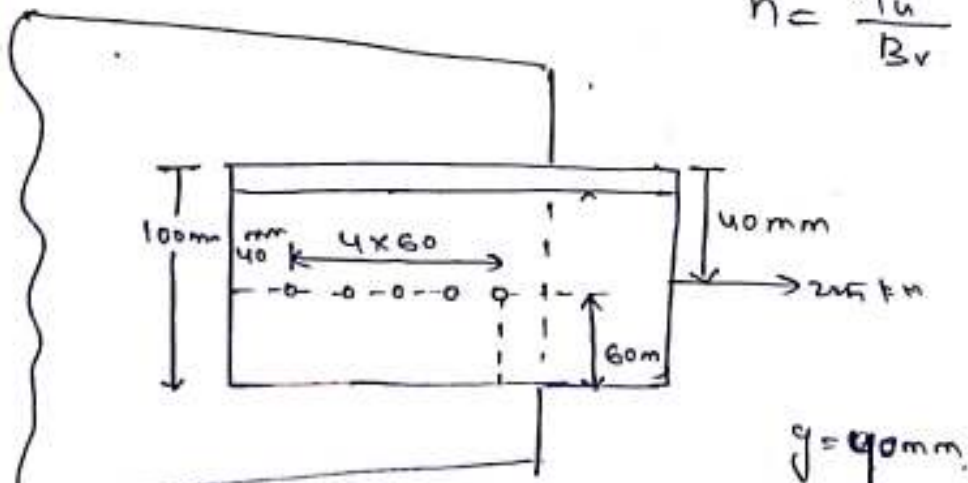
$$= 78.72 \text{ KN}$$

$\therefore \text{Bolt strength} = \min(45.27 \text{ KN}, 78.72 \text{ KN})$

$$B_v = 45.27 \text{ KN}$$

* No of Bolt Required for connection

$$n = \frac{T_u}{B_v} = \frac{225}{45.27} = 4.97 \text{ nos}$$



10

Design Tensile strength of tension member (T_d)

① Design strength due to Gross yielding

$$T_{dg} = \frac{f_y \times A_g}{\gamma_{mo}}$$

$$A_g = 1336 \text{ mm}^2$$

$$T_{dg} = \frac{250 \times 1336}{1.1} \\ = 303.63 \text{ kN.}$$

② Design Rupture strength

$$T_{dr} = \frac{0.9 \times f_u \times A_{nc}}{\gamma_{m1}} + \frac{\beta \times A_{go} \times f_y}{\gamma_{mo}}$$

$$\beta = 1.4 - 0.076 \times \left(\frac{w}{t}\right) \times \left(\frac{f_y}{f_u}\right) \times \left(\frac{b_s}{l_c}\right)$$

$$w = 75 \text{ mm}$$

$$t = 8 \text{ mm}$$

$$b_s = (w + g - t)$$

$$= (75 + 40 - 8)$$

$$= 107 \text{ mm}$$

$$l_c = 4 \times 60 = 240 \text{ mm}$$

$$\beta = 1.4 - 0.076 \times \left(\frac{75}{8}\right) \times \left(\frac{240}{410}\right) \times \left(\frac{107}{240}\right)$$

$$= 1.2$$

check

$$\frac{\gamma_{m0} \times f_u}{\gamma_{m1} \times f_y} = \frac{1.1 \times 410}{1.25 \times 250} = 1.44 \geq 1.2$$

$$0.7 \leq 1.2$$

$$\therefore \beta = 1.2$$

$$\begin{aligned} A_{nc} &= (100 - s/2 - r_1) \times t \\ &= (100 - 8/2 - 22) \times 8 = 592 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} A_{go} &= (75 - s/2) \times t = (75 - 8/2) \times 8 \\ &= 568 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} T_{dn} &= \frac{0.9 \times 592 \times 410}{1.25} + \frac{1.25 \times 568 \times 250}{1.1} \\ &= 379.66 \text{ kN} \end{aligned}$$

② Design block shear strength

$$A_{vn} = (e + 4 \times p - u \cdot r \times d_0) \times t = (40 + 4 \times 60 - 0.5 \times 22) \times 8$$

$$A_{vg} = (e + 4 \times p) \times t = (40 + 4 \times 60) \times 8 = 2240 \text{ mm}^2$$

$$A_{tg} = 60 \times t = 60 \times 8 = 480 \text{ mm}^2$$

$$A_{tn} = (60 - 0.5 \times d_0) \times t = (60 - 0.5 \times 22) \times 8 = 392 \text{ mm}^2$$

$$\begin{aligned} T_{db1} &= \frac{0.9 \times A_{tn} \times f_u}{\gamma_{m1}} + \frac{f_y \times A_{vg}}{\gamma_{m0} \times \sqrt{3}} \\ &= \frac{0.9 \times 392 \times 410}{1.25} + \frac{250 \times 2240}{1.1 \times \sqrt{3}} \end{aligned}$$

$$= 409.64 \text{ kN}$$

$$T_{db1} = \frac{0.9 \times f_u \times A_{vn}}{\sqrt{3} \times \gamma_{m1}} + \frac{f_y \times A_{t1}}{\gamma_{m0}}$$

$$= \frac{0.9 \times 410 \times 1448}{\sqrt{3} \times 1.25} + \frac{250 \times 480}{1.1}$$

$$= 355.87 \text{ kN}$$

$$\therefore T_{db} = \min(T_{db1}, T_{db2})$$

$$T_{db} = 355.87 \text{ kN}$$

\therefore Design tensile strength of tension Member

$$T_d = \min(T_{dg}, T_{dn}, T_{db})$$

$$(T_d = 303.63 \text{ kN})$$

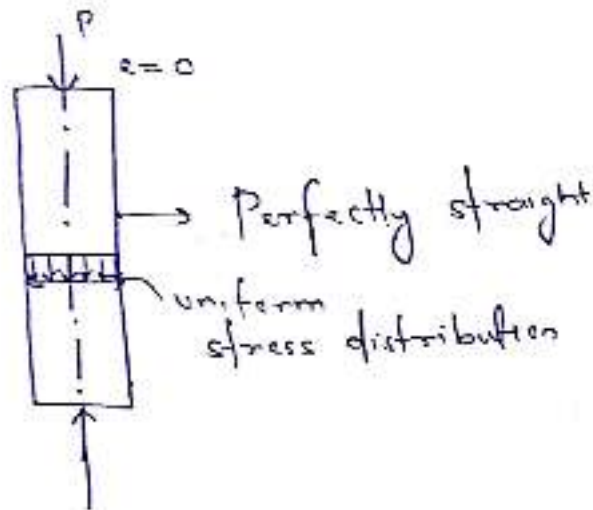
$$T_d = 303.63 > 225 \text{ kN}$$

$$(T_d > T_u)$$

Design is ok

Design of compression Member.

- * A compression member is a straight structural element which is subjected to two compressive forces.



- * An ideal compression member is the one which is-
- Perfectly straight (no initial curvature present inside)
 - load is none eccentric.
 - No residual stresses.
 - No imperfection (crookedness)

Note:- Practically above condition is not exist.

Types of compression member① Columns, stanchions or posts

- * Column is a long vertical compression member which is used to support floor or slab in framed building.

② Strut

* It is an inclined compression member in a truss or a bracing system

Strut are two types

① Continuous struts - when a strut passes through multiple joints.

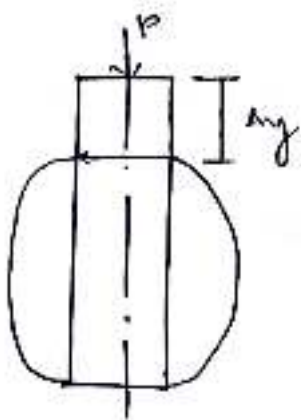
② Discontinuous struts - when a strut spans between two joints only.

③ Principal Rafter

* It is the top most inclined compression member in a roof truss.

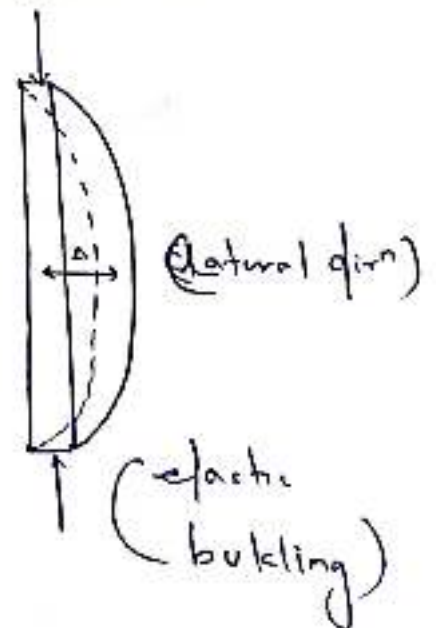
④ Boom:- It is the principal compression element in a gantry crane.

Short column

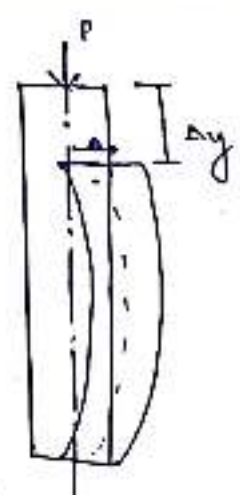


(Yielding or crushing failure)

Long Column



Intermediate column



Yielding + Buckling

(Inelastic Buckling)

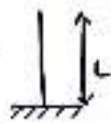





Effective length (Le)

- * It is the length of compression member which undergoes buckling/curvature
- * It can be defined as the length between two points of hinged end.
- * Effective length is depends upon unsupported length of the member and the end support conditions.
- * A every support two types of restrained may exist
 - a) Rotational Restrained θ'
 - b) Lateral sway or translational Restrained. (A)

	Hinged supports	$\theta \rightarrow$ free	$A \rightarrow$ Restrained
	fixed support	$\theta \rightarrow$ Restrained	$A \rightarrow$ Restrained
	Sliding & guided Roller	$\theta \rightarrow$ Restrained	$A \rightarrow$ free.

Acc. IS 800-2007, pg-45, T-11, effective length of prismatic compression member.

Support ends

Support ends				Symbol	Theoretical value (L _e)	IS code (L _e)
At one end		At other end				
B	A	B	A			
1) Restrained	Restrained	free	free		2L	2L
2) Restrained	free	free	Restrained		2L	2L
3) free	restrained	free	Restrained		2L	2L
4) Restrained	Restrained	Restrained	free		L	1.2L
5) Restrained	Restrained	free	Restrained		0.7L	0.8L
Restrained	Restrained	Restrained	Restrained		0.5L	0.65L

Slenderness Ratio

- * This ~~is~~ tendency of the member to fail by buckling is measured by a non-dimensional number or ratio known as slenderness ratio, λ .
- * Longer the length of member for a given area greater will be tendency to fail by buckling and lesser will be its load carrying capacity.
- * Slenderness ratio is measured by the ratio of effective length of the member & Appropriate Radius of gyration, r .

$$\text{Slenderness Ratio } (\lambda) = \frac{L_e}{r} \quad \text{or} \quad \frac{KL}{r}$$

$L \rightarrow$ unsupported length of member

$K \rightarrow$ constant for effective length.

$r \rightarrow$ Radius of gyration.

$$r = \sqrt{\frac{I}{A}}$$

$I =$ Moment of Inertia

$A =$ Cross sectional Area of Section.

* IS code has kept a limitation on the maximum value of slenderness ratio of the member.

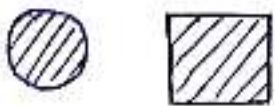
IS - 800-2007, Pg-20, T-3.

<u>Member</u>	<u>Slenderness Ratio</u>
a) A member carrying compressive load from dead & imposed load	180
b) A member subjected to compressive force resulting only from combination with wind/earthquake action	250
c) Compression flange of a beam restrained against torsional buckling	300.

Types of Section

* Generally those section are preferred which provide maximum value of least radius of gyration.

① Bars or Rod

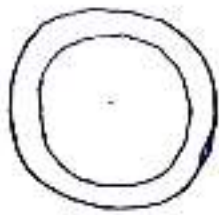


* In case of solid bars most of the area of cross section is located near by to principal axes, due to which they have less value of moment of inertia for a given area.

* They are not preferred if the length of the member is greater than 3m.

(4)

(2) Hollow tube Section



* In this section most of the area is located away from principal axes, Hence they provide high value of moment of inertia / Radius of gyration.

* Hollow Section have good resistance towards torsion also.

* for bracing element hollow section are used.

(3) Single angle Section

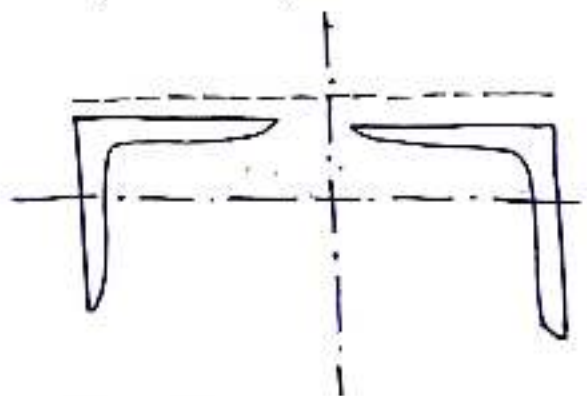
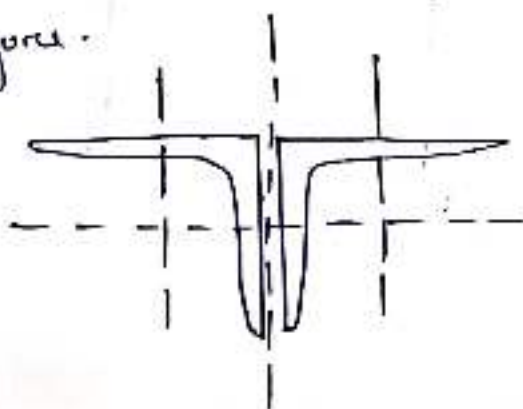
* It can be used as a roof truss element connected with the help of bolting / Riveting or welding

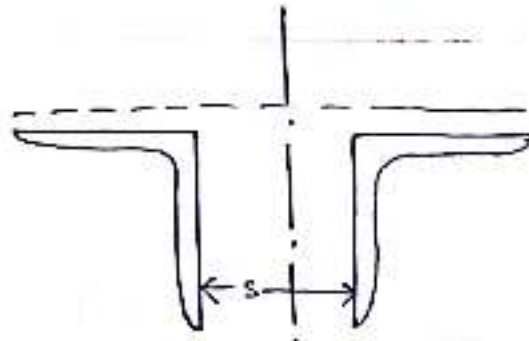
* Equal angles are preferred over unequal angles as they provide larger value of minimum radius of gyration.

(4) Double angle Section

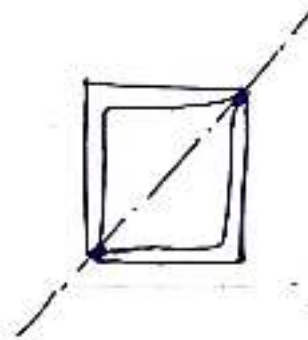
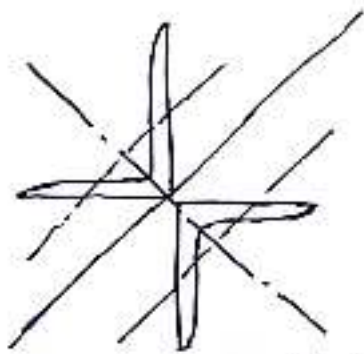
* Strut in a truss are generally made from double angle section connected back to back or spaced apart as shown in

figures.





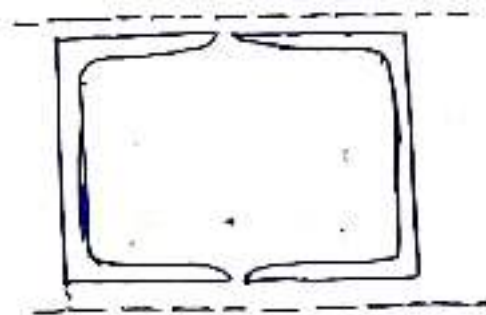
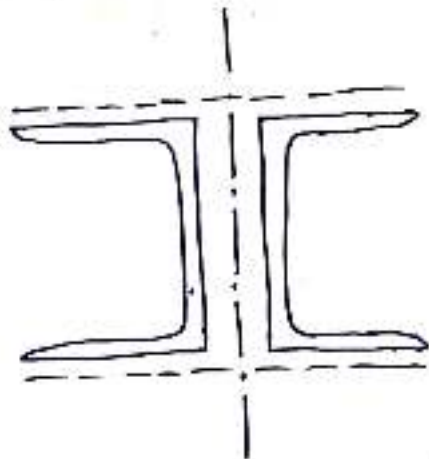
* In case of double angle section connected back to back unequal angle section are preferred, with their longer leg is connected.



(Star pattern or Cruciform)

5) Double Channel Section

* In case of moderate or heavy loaded structure angle section are not used. Double Channel Section are used which can be connected back to back or toe to toe.



5

Types of Buckling

① Flexural Buckling

- * In this buckling the member moves ~~and~~ translates in a lateral direction, without undergoing rotation.
- * This type of failure occurs when the section has large torsional resistance as compared to bending resistance.
- * Those sections which have large moment of inertia about one axis as compared to the other axis fail by flexural buckling.

② Torsional Buckling

- * In this buckling the member rotates about its longitudinal axis.

③ Flexural-torsional Buckling

- * It is a combined failure of member due to flexural and torsion.

Design Strength of Compression Member.

Perry - Robertson Approach.

- * In Perry Robertson approach all the imperfections, Residual, shape of section, buckling axis & Method of fabrication, all these factors are considered.

* In this approach the buckling was classified into 4 categories. such as a, b, c & d.

<u>Buckling class</u>	<u>Description</u>
a	→ quasi-perfection in the member.
b	→ Moderate level of imperfection.
c	→ High level of imperfection.
d	→ extreme level of imperfection.

[Acc. to IS-800-2007, Pg-44, T-10] Buckling class of cross-section.

eg:- I section	$\frac{h}{b_f} > 1.2$	z-z	a
	$z_f \leq 40\text{mm}$	y-y	b.

* Design compressive strength of member

$$P_d = A_e \times f_{cd}$$

where,

A_e = effective sectional Area / Gross area of a section
 f_{cd} = Design Compressive stress.

⑥

The design compressive stress 'f_{cd}' of axially loaded compression members:

$$f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} \leq f_y / \gamma_{mo}$$

where,

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2]$$

λ = non-dimensional effective slenderness ratio.

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{f_y / f_{cc}}$$

f_{cc} = Euler's buckling stress

$$f_{cc} = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$$

where KL/r = effective slenderness ratio or ratio of effective length, KL to appropriate radius of gyration.

α = Imperfection factor (T-2, Pg-35)

γ_{mo} = Partial safety factor

Value of α (Imperfection factor)

Buckling class	a	b	c	d
α	0.21	0.34	0.49	0.76

Design steps for Compression Member.

Given Data \rightarrow Load (P_u), Length of the member & end support condition

Step-1 :- Assume suitable value of slenderness ratio (λ)
(Generally for a column 3-5 m height, slenderness ratio between 40-60 gives satisfactory result).

Step-2 Corresponding to the slenderness ratio (λ) assumed in (step-1) determine ' f_{cd} ' for a particular buckling classes, [IS-800-2007, pg-40, 41, 42 & 43]

Step-3 Determine required Gross sectional Area.

$$A_g = \frac{P_u}{f_{cd}}$$

Step-4 from IS hand book no. 1 a suitable section is selected which provides the required area A_c per step 3.

Step-5 Determine actual slenderness ratio of the member

$$\lambda = \frac{KL}{r_{min}}$$

\therefore Check the above value of slenderness ratio $\nless \lambda_{max}$
(Given IS code pg-20-T-3)

Step-6 Determine the actual value of slenderness ' f_{cd} ' for the section selected.

$$f_{cd} = \frac{f_y / r_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} \leq f_y / r_{mo}$$

$$\phi = 0.5 [1 + \alpha(\lambda - 0.2) + \lambda^2], \quad \lambda = \sqrt{\frac{f_y}{f_{cc}}}$$

$$f_{cc} = \frac{\lambda^2 E}{KL/r}$$

Step-7 Determine the design compressive strength of Member (P_d)
 $P_d = f_{cd} \times A_c \geq P_u$ (Factored or design load)

7.

Question-1

Determine the design axial load capacity of the column ISHB 300 @ 577 N/m. If the length of the column is 3m and its both end are pinned.

m for rolled steel section ISHB 300 @ 577 N/m

$A_g = 24.85 \text{ cm}^2 = 2485 \text{ mm}^2$ (from steel table)

$h = 300 \text{ mm}$

$b_f = 250 \text{ mm}$

$t_f = 10.6 \text{ mm}$

$f_y = 250 \text{ N/mm}^2$

$f_u = 410 \text{ N/mm}^2$

effective length of column

$L_e = L$ (both end hinged)

$E = 2 \times 10^5 \text{ N/mm}^2$

Minimum radius of gyration

$r_{min} = 54.1 \text{ mm}$

* Buckling classes of cross section

$\rightarrow \frac{h}{b_f} = \frac{300}{250} \leq 1.2$

$\rightarrow t_f = 10.6 \text{ mm} \leq 100 \text{ mm}$

for y-y axis

Buckling class - C (IS 800:2007 pg-44)

Design compressive strength

$T_d = A_e \times f_{cd}$

$\alpha = 0.49$ [code book pg-35] Imperfection factor

$f_{cd} = \frac{\alpha^2 E}{(KL/r)^2} = \frac{\alpha^2 \times 2 \times 10^5}{\left(\frac{3000}{54.1}\right)^2} = 611.92 \text{ N/mm}^2$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{641.92}} = 0.624$$

$$\begin{aligned}\phi &= 0.5 [1 + \alpha(\lambda - 0.2) + \lambda^2] \\ &= 0.5 [1 + 0.41(0.624 - 0.2) + 0.624^2] \\ &= 0.915\end{aligned}$$

Design compressive stress

$$f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} = \frac{250 / 1.1}{0.915 + [0.915^2 - 0.624^2]^{0.5}}$$

$$= 143.46 \leq f_y / \gamma_{mo}$$

$$\leq \frac{250}{1.1} = 227.27 \text{ MPa}$$

\therefore Design compressive strength of column

$$P_d = A_e \times f_{cd}$$

$$= 143.46 \times 7854 = 112673 \text{ kN}$$

Question - 2

Calculate the design compressive load for an ISHB 250 @ 4m height the column is restrained in translation only of both the ends. It is to be used as uncased column in a single story building.

ISHB 250 @ 536.5 N/m

(from steel table)

$$h = 250 \text{ mm}$$

$$b_f = 250 \text{ mm}$$

$$t_f = 9.7 \text{ mm}$$

$$L_e = 0.65L \text{ (Both end fixed)}$$

$$= 0.65 \times 4000$$

$$= 2600 \text{ mm}$$

$$r_{min} = 53.7 \text{ mm}$$

$$A_g = 6971 \text{ mm}^2$$

$$f_y = 250, f_u = 410 \text{ N/mm}^2$$

(8)

Buckling class

$$\rightarrow \frac{b}{b_f} = \frac{250}{250} \leq 1.2$$

$$\rightarrow d_f = 97 < 100 \text{ mm}$$

Buckling class

$$y-y \text{ dir}^n = c$$

$$\therefore \alpha = 0.49 \text{ [IS cod] (pg-22)}$$

$$f_{cc} = \frac{\pi^2 E}{\left(\frac{kL}{r}\right)^2} = \frac{\pi^2 \times 2710^5}{\left(\frac{2600}{53.7}\right)^2} = 842.02 \text{ N/mm}^2$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{842.02}} = 0.544$$

$$\begin{aligned} \phi &= 0.5 \times [1 + \alpha(\lambda - 0.2) + \lambda^2] \\ &= 0.5 \times [1 + 0.49(0.544 - 0.2) + 0.544^2] \\ &= 0.732 \end{aligned}$$

$$f_{cd} = \frac{f_y / \gamma_{m0}}{\phi + (\phi^2 - \lambda^2)^{0.5}}$$

$$= \frac{250/1.1}{0.732 + [0.732^2 - 0.544^2]^{0.5}}$$

$$= 186.017 \text{ N/mm}^2 \leq f_y / \gamma_{m0} = 227.7 \text{ N/mm}^2$$

Design Compressive strength

$$P_d = A_c \times f_{cd}$$

$$= 6971 \times 186.017 = 1296.724 \text{ kN}$$

Design problem

Design a single angle strut connected to the gusset plate to carry 180 kN factored load. The length of the strut is 3m, and its one end is fixed and other end is hinged.

Data given

$$P_u = 180 \text{ kN}, \quad L = 3 \text{ m}$$

$$\text{effective length} = 0.8L = 0.8 \times 3 = 2.4 \text{ m} \quad \left(\begin{array}{l} \text{One end fixed} \\ \text{Other end hinged} \end{array} \right)$$

Step-1 Assume slenderness ratio

$$\lambda = 40$$

Step-2 $\lambda = 40$, buckling class cross-section = c (angle section)

$$\left[\begin{array}{l} \text{IS 800-2007} \\ \text{Pg-42} \\ \text{T-9} \\ f_y = 250 \text{ N/mm}^2 \end{array} \right] \quad \underline{f_{cd} = 198 \text{ N/mm}^2}$$

Step-3 Gross Area required

$$A_g = \frac{P_u}{f_{cd}} = \frac{180 \times 10^3}{198} = 909.09 \text{ mm}^2$$

Step-4

Select ISA 70x70x8 mm (from steel table)
Pg-10

$$A_g = 10.58 \text{ cm}^2 = 1058 \text{ mm}^2$$

Step-5

$$\text{min}^m \text{ radius of gyration } r_{\min} = 1.35 \text{ cm} \\ = 13.5 \text{ mm}$$

9.

$$\text{Slenderness Ratio } (\lambda) = \frac{KL}{r_{\min}}$$

$$= \frac{2400}{13.5} = 177.77 < \lambda_{\max} (180) \text{ (OK)}$$

(IS code T-3)

Step-6 Design Compressive stress 'f_{cd}'
 $\alpha = 0.49$ Buckling class 'c'

$$f_{cc} = \frac{\pi^2 E}{(KL/r)^2} = \frac{\pi^2 \times 2 \times 10^5}{(177.77)^2} = 62.01 \text{ N/mm}^2$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{62.01}} = 2$$

$$\phi = 0.8 \times [1 + \alpha(\lambda - 0.2) + \lambda^2]$$

$$= 0.8 [1 + 0.49(2 - 0.2) + 2^2]$$

$$= 2.941$$

$$f_{cd} = \frac{f_y / \gamma_{m0}}{\phi + [\alpha^2 - \lambda^2]^{0.5}}$$

$$= \frac{250 / 1.1}{2.941 + [2.941^2 - 2^2]^{0.5}}$$

$$= 44.587 \leq f_y / \gamma_{m0} = 227.27 \text{ N/mm}^2$$

Step-7 Design Compressive strength of column

$$P_d = A_c \times f_{cd}$$

$$= 1058 \times 44.587 = 47173 \text{ kN} > P_u = 150 \text{ kN}$$

OK